

Disequazioni goniometriche fratte

1	$\frac{\sin x}{1 - 2 \sin x} > 0$	$2\kappa\pi < x < \frac{\pi}{6} + 2\kappa\pi \quad \vee$ $\frac{5}{6}\pi + 2\kappa\pi < x < \pi + \kappa\pi$
2	$\frac{\sin x}{\cos x} + \sqrt{3} \leq 0$	$\frac{\pi}{4} + \kappa\pi < x < \frac{\pi}{2} + \kappa\pi \quad \vee$ $\frac{2}{3}\pi + \kappa\pi < x < \frac{3}{4}\pi + 2\kappa\pi$
3	$\frac{2 \sin^2 x + 1}{\cos 2x} < 0$	$\frac{\pi}{4}\kappa\pi < x < \frac{3}{4}\pi + \kappa\pi$
4	$1 - \frac{1}{\tan x} > 0$	$\frac{\pi}{4} + \kappa\pi < x < \frac{\pi}{2} + \kappa\pi \quad \vee$ $\frac{\pi}{2} + \kappa\pi < x < \pi + \kappa\pi$
5	$\frac{\sin x}{\sin x + 1} > 1$	impossibile
6	$\frac{1 - \cos x}{\sin x \cos x} \geq 0$	$\kappa\pi < x < \frac{\pi}{2} + \kappa\pi$
7	$\frac{1}{\cot x} + \frac{1}{\tan x} < \frac{4}{3}$	$\frac{\pi}{2} + \kappa\pi < x < \pi + \kappa\pi$
8	$\frac{2 \sin x + 1}{\cos x} \geq 0$	$\frac{\pi}{6} + 2\kappa\pi \leq x < \frac{\pi}{2} + 2\kappa\pi \quad \vee$ $\frac{7}{6}\pi + 2\kappa\pi \leq x < \frac{3}{2}\pi + 2\kappa\pi$
9	$\frac{\tan x - 1}{\tan x} < 0$	$\kappa\pi < x < \pi + 2\kappa\pi$
10	$\frac{\sin x}{\cos x + 1} \geq 0$	$2\kappa\pi < x < \pi + 2\kappa\pi$
11	$\frac{1 - 2\cos x}{\tan x} \leq 0$	$2\kappa\pi < x \leq \frac{\pi}{3} + 2\kappa\pi \quad \vee$ $\frac{\pi}{2} + 2\kappa\pi < x < \pi + 2\kappa\pi$ $\vee \frac{3}{2}\pi + 2\kappa\pi < x \leq \frac{5}{3}\pi + 2\kappa\pi$
12	$\frac{2 \sin x - \sqrt{3}}{2 \cos x + 1} > 0$	$\frac{\pi}{3} + 2\kappa\pi \leq x \frac{4}{3}\pi + 2\kappa\pi \quad \vee$ $x \neq \frac{2}{3}\pi + 2\kappa\pi$
13	$\frac{\cos^2 x - \sin^2 x}{\cos x \cos 3x} < 0$	$\frac{\pi}{2} + 2\kappa\pi < x < \frac{3}{2}\pi + 2\kappa\pi \quad \vee$ $x \neq \frac{3}{4}\pi + 2\kappa\pi \quad \vee \quad x \neq \frac{5}{4}\pi + 2\kappa\pi$
14	$\frac{\sin 6x - \sin 2x}{(\cos 2x + \sin 2x)(\cos 2x - \sin 2x)} \geq 0$	$\kappa\pi \leq x \leq \frac{\pi}{2} + \kappa\pi \quad \vee \quad x \neq \frac{\pi}{8} + \kappa\frac{\pi}{4}$
15	$\frac{2 \sin x \cos^2 x}{\cos 3x + \cos x} \geq 0$	$\kappa\frac{\pi}{2} \leq x < \frac{\pi}{4} + \kappa\frac{\pi}{2} \quad \vee \quad x \neq \frac{\pi}{2} + \kappa\pi$

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16	$\frac{2 \sin x + \sqrt{2}}{\tan x - \sqrt{3}} \leq 0$	$\begin{aligned} -\frac{\pi}{4} + 2k\pi &\leq x < \frac{\pi}{3} + 2k\pi & \vee \\ \frac{\pi}{2} + 2k\pi &< x \leq \frac{5}{4}\pi + 2k\pi & \vee \\ \frac{4}{3}\pi + 2k\pi &< x < \frac{3}{2}\pi + 2k\pi \end{aligned}$
17	$\frac{2 \cos x - 3}{\sin x} \geq 0$	$\pi + 2k\pi < x < 2\pi + 2k\pi$
18	$\frac{1 + \sin^2 \left(x + \frac{\pi}{3} \right)}{1 - \cot^2 \left(\frac{\pi}{6} - x \right)} > 0$	$-\frac{7}{12}\pi + k\pi < x < -\frac{\pi}{12} + k\pi$
19	$\frac{4 \sin^2 x - 1}{2 \cos x} \geq 0$	$\begin{aligned} \frac{\pi}{6} + 2k\pi &< x < \frac{\pi}{2} + 2k\pi \\ \vee \quad \frac{5}{6}\pi + 2k\pi &\leq x < \frac{7}{6}\pi + 2k\pi \\ \frac{3}{2}\pi + 2k\pi &< x \leq \frac{11}{6}\pi + 2k\pi \end{aligned}$
20	$\frac{4 \cos^2 x - 3}{2 \sin x - 1} > 0$	$\frac{7}{6}\pi + 2k\pi < x < \frac{11}{6}\pi + 2k\pi$
21	$\frac{2 \sin x - 1}{\sin x} > 0$	$\begin{aligned} 2k\pi &< x < \frac{\pi}{2} + 2k\pi \vee \\ \frac{\pi}{2} + 2k\pi &< x < \pi + 2k\pi \end{aligned}$
22	$\frac{\sin x + \sqrt{3}}{\sin x} \geq 3$	$\begin{aligned} 2k\pi &< x \leq \frac{\pi}{3} + 2k\pi \vee \\ \frac{2}{3}\pi + 2k\pi &\leq x < \pi + 2k\pi \end{aligned}$
23	$\frac{\sqrt{3} \tan x - 1}{2 \sin x - \sqrt{3}} < 0$	$\begin{aligned} \frac{\pi}{6} + 2k\pi &< x < \frac{\pi}{3} + 2k\pi \\ \frac{\pi}{2} + 2k\pi &< x < \frac{2}{3}\pi + 2k\pi \\ \frac{7}{6}\pi + 2k\pi &< x < \frac{3}{2}\pi + 2k\pi \end{aligned}$
24	$\frac{\sin 2x}{\sin x (2 \sin x - \sqrt{2})} \leq 0$	$\begin{aligned} 0 < x < \frac{\pi}{4} \vee \quad \frac{\pi}{2} &\leq x < \frac{3}{4}\pi \vee \\ \frac{3}{2}\pi &\leq x < 2k\pi \end{aligned}$