

# Formule goniometriche

| addizione e sottrazione  |  |
|--|--|
| $\sin(\alpha + \beta) = \sin(\alpha) \cdot \cos(\beta) + \sin(\beta) \cdot \cos(\alpha)$ | $\tan(\alpha + \beta) = \frac{\tan(\alpha) + \tan(\beta)}{1 - \tan(\alpha) \cdot \tan(\beta)}$ |
| $\sin(\alpha - \beta) = \sin(\alpha) \cdot \cos(\beta) - \sin(\beta) \cdot \cos(\alpha)$ | $\tan(\alpha - \beta) = \frac{\tan(\alpha) - \tan(\beta)}{1 + \tan(\alpha) \cdot \tan(\beta)}$ |
| $\cos(\alpha + \beta) = \cos(\alpha) \cdot \cos(\beta) - \sin(\alpha) \cdot \sin(\beta)$ | $\cot(\alpha + \beta) = \frac{\cot(\alpha) \cdot \cot(\beta) - 1}{\cot(\beta) + \cot(\alpha)}$ |
| $\cos(\alpha - \beta) = \cos(\alpha) \cdot \cos(\beta) + \sin(\alpha) \cdot \sin(\beta)$ | $\cot(\alpha - \beta) = \frac{\cot(\alpha) \cdot \cot(\beta) + 1}{\cot(\beta) - \cot(\alpha)}$ |

| duplicazione                                       |   |
|--|---|
| $\sin(2\alpha) = 2\sin(\alpha) \cdot \cos(\alpha)$ | $\tan(2\alpha) = \frac{2 \tan(\alpha)}{1 - \tan^2(\alpha)} = \frac{2}{\cot(\alpha) - \tan(\alpha)}$ |
| $\cos(2\alpha) = \cos^2(\alpha) - \sin^2(\alpha)$  | $\cot(2\alpha) = \frac{\cot^2(\alpha) - 1}{2 \cot(\alpha)} = \frac{\cot(\alpha) - \tan(\alpha)}{2}$ |
| $\cos(2\alpha) = 2\cos^2(\alpha) - 1$              |   |

| bisezione   |  |
|---|--|
| $\sin\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos(\alpha)}{2}}$ | $\tan\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos(\alpha)}{1 + \cos(\alpha)}} = \frac{\sin(\alpha)}{1 + \cos(\alpha)} = \frac{1 - \cos(\alpha)}{\sin(\alpha)}$ |
| $\cos\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos(\alpha)}{2}}$ | $\cot\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos(\alpha)}{1 - \cos(\alpha)}} = \frac{\sin(\alpha)}{1 - \cos(\alpha)} = \frac{1 + \cos(\alpha)}{\sin(\alpha)}$ |

| parametriche o razionali $t = \tan\left(\frac{\alpha}{2}\right)$ |                                     |
|--|-------------------------------------|
| $\sin(\alpha) = \frac{2t}{1 + t^2}$                              | $\tan(\alpha) = \frac{2t}{1 - t^2}$ |
| $\cos(\alpha) = \frac{1 - t^2}{1 + t^2}$                         | $\cot(\alpha) = \frac{1 - t^2}{2t}$ |

| prostaferesi  |  |
|---|--|
| $\sin(p) + \sin(q) = 2 \sin\frac{p+q}{2} \cdot \cos\frac{p-q}{2}$ | $\sin(p) - \sin(q) = 2 \sin\frac{p-q}{2} \cdot \cos\frac{p+q}{2}$  |
| $\cos(p) + \cos(q) = 2 \cos\frac{p+q}{2} \cdot \cos\frac{p-q}{2}$ | $\cos(p) - \cos(q) = -2 \sin\frac{p+q}{2} \cdot \sin\frac{p-q}{2}$ |

| Werner   |  |
|--|--|
| $\sin(\alpha) \cdot \sin(\beta) = \frac{\cos(\alpha - \beta) - \cos(\alpha + \beta)}{2}$ | $\sin(\alpha) \cdot \cos(\beta) = \frac{\sin(\alpha - \beta) + \sin(\alpha + \beta)}{2}$ |
| $\cos(\alpha) \cdot \cos(\beta) = \frac{\cos(\alpha - \beta) + \cos(\alpha + \beta)}{2}$ |  |