

# Razionalizzazione

razionalizza i denominatori delle seguenti frazioni

1	$\frac{2}{\sqrt{2}}$	$\frac{1}{\sqrt{5}}$	$\frac{2}{\sqrt{12}}$	$\sqrt{2}$	$\frac{\sqrt{5}}{5}$	$\frac{\sqrt{3}}{3}$
2	$\frac{2\sqrt{7}}{\sqrt{20}}$	$\frac{2\sqrt{3}}{\sqrt{18}}$	$\frac{8\sqrt{5}}{3\sqrt{28}}$	$\frac{\sqrt{35}}{5}$	$\frac{\sqrt{6}}{3}$	$\frac{4\sqrt{35}}{21}$
3	$\frac{2\sqrt{15}}{3\sqrt{75}}$	$\frac{\sqrt[3]{3}}{\sqrt{5}}$	$\frac{\sqrt{5} - \sqrt{3}}{3\sqrt{2}}$	$\frac{2\sqrt{5}}{15}$	$\frac{\sqrt[6]{1125}}{5}$	$\frac{\sqrt{10} - \sqrt{6}}{6}$
4	$\frac{2\sqrt{2} - 3\sqrt{5}}{2\sqrt{3}}$			$\frac{2\sqrt{6} - 3\sqrt{15}}{6}$		
5	$\frac{2\sqrt{40} - 3\sqrt{8} - \sqrt{5}}{6\sqrt{12}}$			$\frac{\sqrt{3}(4\sqrt{10} - 6\sqrt{2} - \sqrt{5})}{36}$		
6	$\frac{\sqrt{50} + \sqrt{12} - 3\sqrt{2}}{4\sqrt{8}}$			$\frac{\sqrt{2}(\sqrt{3} + \sqrt{2})}{8}$		
7	$\frac{a}{2\sqrt{a}}$	$\frac{a^2 - b^2}{\sqrt{a+b}}$		$\frac{\sqrt{a}}{2}$		$(a-b)\sqrt{a+b}$
8	$\frac{4a\sqrt[3]{ab}}{\sqrt{b}}$	$\frac{a+5}{\sqrt{a+5}}$		$\frac{4\sqrt[6]{a^8b^5}}{b}$		$\sqrt{a+5}$
9	$\frac{\sqrt{x} - \sqrt{y}}{\sqrt{y}}$	$\frac{x-y}{\sqrt{x^2-y^2}}$		$\frac{\sqrt{xy}}{y} - 1$		$\frac{\sqrt{x^2-y^2}}{x+y}$
10	$\frac{x^2 + 2x + 1}{\sqrt{x+1}}$				$(x+1)\sqrt{x+1}$	
11	$\frac{x^3 - 8}{\sqrt{x-2}}$				$(x^2 + 2x + 4)\sqrt{x-2}$	
12	$\frac{3}{\sqrt{a^3}}$	$\frac{2}{\sqrt[3]{4}}$	$\frac{2}{\sqrt[3]{8}}$	$\frac{3\sqrt{a}}{a^2}$	$\sqrt[3]{2}$	$\frac{\sqrt[5]{4}}{3}$
13	$\frac{\sqrt{x^3} \cdot \sqrt[14]{x^5}}{x^7\sqrt{x^6}}$	$\frac{4\sqrt{3}}{\sqrt[7]{9}}$	$\frac{3\sqrt{2}}{4\sqrt[3]{2}}$	1	$4\sqrt[14]{27}$	$\frac{3\sqrt[6]{2}}{4}$
14	$\frac{12}{7\sqrt[6]{18}}$	$\frac{x}{\sqrt[4]{xy}}$	$\frac{6}{5\sqrt[3]{a^2b}}$	$\frac{2\sqrt[6]{2592}}{7}$	$\frac{\sqrt[4]{x^3y^3}}{y}$	$\frac{6\sqrt[3]{a^2b^4}}{5a^2b}$
15	$\frac{8abc}{3\sqrt[4]{a^3b^2c}}$	$\frac{xy^3z}{\sqrt[5]{x^2y^7z}}$		$\frac{8\sqrt[4]{ab^2c^3}}{3}$	$y\sqrt[5]{x^3y^3z^4}$	

16	$\frac{3ax}{2b\sqrt[5]{a^3x}}$	$\frac{a^2bxy^3}{\sqrt[6]{a^5xy^5}}$	$\frac{3\sqrt[5]{a^2x^4}}{2b} \quad aby^2\sqrt[6]{ax^5y}$
17	$\frac{b}{y\sqrt[5]{b^3}}$	$\frac{4xy - 4y^2}{2\sqrt[3]{x^2 - 2xy + y^2}}$	$\frac{\sqrt[5]{b^2}}{y} \quad 2y\sqrt[3]{x - y}$
18	$\frac{a^2b}{x\sqrt[3]{axb}}$	$\frac{4x^2y(x - y)}{\sqrt[3]{16x^4y^2(x - y)^2}}$	$\frac{\sqrt[3]{a^5x^2b^2}}{x^2} \quad \sqrt[3]{4x^2y(x - y)}$
19	$\frac{x^3 - y^3}{(x^2 + xy + y^2)\sqrt[4]{x - y}}$	$\frac{a+b}{\sqrt[5]{a^2+2ab+b^2}}$	$\sqrt[4]{(x - y)^3} \quad \sqrt[5]{(a + b)^3}$
20	$\frac{(x+y)^2}{\sqrt[4]{x+y}}$		$(x+y)\sqrt[4]{(x+y)^3}$
21	$\frac{a^2 - 1}{\sqrt[3]{(a^2 - 2a + 1)^2}}$		$\frac{(a+1)\sqrt[3]{a-1}}{a-1}$
22	$\frac{a^2 - b^2}{\sqrt[3]{a+b}}$		$(a-b)\sqrt[3]{(a+b)^2}$
23	$\frac{\sqrt{xy} + \sqrt[3]{xy^2}}{\sqrt[3]{x} \cdot \sqrt{y}}$		$\sqrt[6]{x} + \sqrt[6]{y}$
24	$\frac{2}{\sqrt{3} + \sqrt{2}}$		$2(\sqrt{3} - \sqrt{2})$
25	$\frac{5}{4 - \sqrt{5}}$		$\frac{5(4 + \sqrt{5})}{11}$
26	$\frac{6}{2 + \sqrt{2}}$		$3(2 - \sqrt{2})$
27	$\frac{6}{\sqrt{6} - \sqrt{2}}$		$\frac{3\sqrt{2}(\sqrt{3} + 1)}{2}$
28	$\frac{3\sqrt{3}}{\sqrt{3} - 3}$		$-\frac{3(\sqrt{3} + 1)}{2}$
29	$\frac{\sqrt{7} + 2}{\sqrt{7} - 2}$		$\frac{11 + 4\sqrt{7}}{3}$
30	$\frac{a - b}{b - \sqrt{ab}}$		$\frac{-b + \sqrt{ab}}{b}$
31	$\frac{\sqrt{a} - a\sqrt{a}}{1 - \sqrt{a}}$		$\sqrt{a} + a$

32	$\frac{12}{\sqrt{3} - \sqrt{2}}$	$12(\sqrt{3} + \sqrt{2})$
33	$\frac{\sqrt{7} + 2\sqrt{3}}{19 + 4\sqrt{21}}$	$\frac{2\sqrt{3} - \sqrt{7}}{5}$
34	$\frac{\sqrt{a} - \sqrt{2}}{\sqrt{a} + \sqrt{2}}$	$\frac{a + 2 - 2\sqrt{2a}}{a - 2}$
35	$\frac{a - b}{\sqrt{a} - \sqrt{b}}$	$\sqrt{a} + \sqrt{b}$
36	$\frac{\sqrt{x} - \sqrt{y}}{\sqrt{x} + \sqrt{y}}$	$\frac{x + y - 2\sqrt{xy}}{x - y}$
37	$\frac{8}{\sqrt{2a} + 2b}$	$\frac{4(\sqrt{2a} - 2b)}{a - 2b^2}$
38	$\frac{\sqrt{x}}{\sqrt{x} - 2\sqrt{y}}$	$\frac{x + 2\sqrt{xy}}{x - 4y}$
39	$\frac{a - 2}{2\sqrt{a} - a\sqrt{2}}$	$-\frac{2\sqrt{a} + a\sqrt{2}}{2a}$
40	$\frac{a + 2\sqrt{ab} + b}{\sqrt{a} + \sqrt{b}}$	$\sqrt{a} + \sqrt{b}$
41	$\frac{a - 5\sqrt{a} + b}{\sqrt{a} - 2}$	$\sqrt{a} - 3$
42	$\frac{3ab}{\sqrt{3a} - \sqrt{ab}}$	$\frac{3b(\sqrt{3a} + \sqrt{ab})}{3 - b}$
43	$\frac{x^2 - 2xy + y^2}{\sqrt{x} - \sqrt{y}}$	$(x - y)(\sqrt{x} + \sqrt{y})$
44	$\frac{ab}{(\sqrt{a - b} + \sqrt{a + b})}$	$\frac{-a(\sqrt{a - b} - \sqrt{a + b})}{2}$
45	$\frac{\sqrt{a + b} + \sqrt{a - b}}{\sqrt{a + b} - \sqrt{a - b}}$	$\frac{a + \sqrt{a^2 - b^2}}{b}$
46	$\frac{a + 3 + 2\sqrt{a + 2}}{\sqrt{a + 2} + 1}$	$1 + \sqrt{a + 2}$

47	$\frac{a+1}{\sqrt{a+4}-\sqrt{3}}$	$\sqrt{a+4}+\sqrt{3}$
48	$\frac{3b+3}{\sqrt{2b+3}-\sqrt{b+2}}$	$3(\sqrt{2b+3}+\sqrt{b+2})$
49	$\frac{\sqrt{ab}}{\sqrt{a^2b^3}+\sqrt{a^5b}}$	$\frac{b\sqrt{a}-a^2}{b^2-a^3}$
50	$\frac{3\sqrt{3}}{2-\sqrt{2}+\sqrt{3}}$	$\frac{36\sqrt{2}-15\sqrt{6}+27+6\sqrt{3}}{23}$
51	$\frac{23\sqrt{6}}{\sqrt{3}-\sqrt{2}-2}$	$9\sqrt{2}-10\sqrt{3}-2\sqrt{6}-24$
52	$\frac{3\sqrt{3}}{2-\sqrt{2}+\sqrt{3}}$	$\frac{36\sqrt{2}-15\sqrt{6}+27+6\sqrt{3}}{23}$
53	$\frac{1-\sqrt{2}}{\sqrt{2}-\sqrt{3}-\sqrt{5}}$	$\frac{2\sqrt{15}-6-\sqrt{30}+3\sqrt{2}-2\sqrt{3}+2\sqrt{6}}{12}$
54	$\frac{1}{\sqrt{3}+\sqrt{5}-\sqrt{2}}$	$\frac{\sqrt{30}-3\sqrt{2}+2\sqrt{3}}{12}$
55	$\frac{4}{\sqrt{2}-\sqrt{3}-\sqrt{6}}$	$\frac{4(7\sqrt{2}-5\sqrt{3}+\sqrt{6}-12)}{23}$
56	$\frac{3}{\sqrt{7}-\sqrt{2}+\sqrt{3}}$	$\frac{3(\sqrt{42}-4\sqrt{2}+3\sqrt{3}-\sqrt{7})}{10}$
57	$\frac{2\sqrt{2}-\sqrt{3}}{\sqrt{2}-\sqrt{3}+\sqrt{6}}$	$-\frac{17\sqrt{6}-27\sqrt{2}+16\sqrt{3}-43}{23}$
58	$\frac{15\sqrt{2}}{\sqrt{6}+\sqrt{2}-2\sqrt{3}}$	$\frac{15(4+2\sqrt{3}+\sqrt{6}+3\sqrt{2})}{4}$
59	$\frac{2}{\sqrt{3}+\sqrt{5}-\sqrt{2}}$	$\frac{2\sqrt{3}-3\sqrt{2}+\sqrt{30}}{6}$
60	$\frac{\sqrt{2}-\sqrt{3}+1}{\sqrt{3}+1+\sqrt{6}}$	$\sqrt{2}-\sqrt{3}+\sqrt{6}-2$
61	$\frac{2\sqrt{2}+3}{\sqrt{6}+\sqrt{3}+\sqrt{2}+2}$	$\sqrt{6}+\sqrt{3}-\sqrt{2}-2$

62	$\frac{1}{\sqrt{6} - \sqrt{2} + \sqrt{3} - 1}$	$\frac{\sqrt{6} - \sqrt{3} + \sqrt{2} - 1}{2}$
63	$\frac{\sqrt{3}}{2 - \sqrt{6} - \sqrt{2} + \sqrt{3}}$	$-3\sqrt{2} - 2\sqrt{3} - \sqrt{6} - 3$
64	$\frac{1}{\sqrt[3]{3} - 2}$	$-\frac{\sqrt[3]{9} + 2\sqrt[3]{3} + 4}{5}$
65	$\frac{\sqrt[3]{2}}{\sqrt[3]{2} - 1}$	$(1 + \sqrt[3]{4} + \sqrt[3]{2})^3\sqrt{2}$
66	$\frac{3}{\sqrt[3]{5} - \sqrt[3]{2}}$	$\sqrt[3]{25} + \sqrt[3]{10} + \sqrt[3]{4}$
67	$\frac{a + b^3}{\sqrt[3]{a} + b}$	$\sqrt[3]{a^2} - b^3\sqrt[3]{a} + b^2$
68	$\frac{3\sqrt[3]{2}}{\sqrt[3]{2} - 1}$	$3(2 + \sqrt[3]{4} + \sqrt[3]{2})$
69	$\frac{6}{\sqrt[3]{3} - \sqrt[3]{2}}$	$6(\sqrt[3]{9} + \sqrt[3]{6} + \sqrt[3]{4})$
70	$\frac{13}{2 - \sqrt[4]{3}}$	$(2 + \sqrt[4]{3})(4 + \sqrt{3})$
71	$\frac{10}{2\sqrt[3]{2} - \sqrt[3]{6}}$	$4\sqrt[3]{4} + 2\sqrt[3]{12} + \sqrt[3]{36}$
72	$\frac{19}{2\sqrt[3]{3} - \sqrt[3]{5}}$	$4\sqrt[3]{9} + 2\sqrt[3]{15} + \sqrt[3]{25}$
73	$\frac{13}{2\sqrt[3]{3} + \sqrt[3]{2}}$	$\frac{4\sqrt[3]{9} - 2\sqrt[3]{6} + \sqrt[3]{4}}{2}$
74	$\frac{y}{\sqrt[3]{x+y} - \sqrt[3]{x}}$	$\sqrt[3]{(x+y)^2} + \sqrt[3]{x^2+xy} + \sqrt[3]{x^2}$
75	$\frac{2x}{\sqrt[3]{x+y} + \sqrt[3]{x-y}}$	$\sqrt[3]{(x+y)^2} - \sqrt[3]{x^2-y^2} + \sqrt[3]{(x-y)^2}$
76	$\frac{5x}{\sqrt[3]{5x+2} - \sqrt[3]{2}}$	$\sqrt[3]{(5x+2)^2} + \sqrt[3]{10x+4} + \sqrt[3]{4}$