

# Disequazioni goniometriche fratte

1	$\frac{\sin x}{1+2\cos x} > 0$	$2k\pi < x < \frac{2}{3}\pi + 2k\pi \vee \pi + 2k\pi < x < \frac{4}{3}\pi + 2k\pi$
2	$\frac{1+\tan x}{\cos x} \geq 0$	$2k\pi \leq x \leq \frac{3}{4}\pi + 2k\pi \wedge x \neq \frac{\pi}{2} + 2k\pi \vee \frac{7}{4}\pi + 2k\pi \leq x \leq 2\pi + 2k\pi$
3	$\frac{2\sin x + \sqrt{2}}{\cos x} < 0$	$\frac{\pi}{2} + 2k\pi < x < \frac{5}{4}\pi + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x < \frac{7}{4}\pi + 2k\pi$
4	$\frac{2\sin x + 1}{2\cos x + \sqrt{2}} \geq 0$	$2k\pi \leq x < \frac{3}{4}\pi + 2k\pi \vee \frac{7}{6}\pi + 2k\pi \leq x < \frac{5}{4}\pi + 2k\pi \vee \frac{11}{6}\pi + 2k\pi \leq x \leq 2\pi + 2k\pi$
5	$\frac{3\cot x + \sqrt{3}}{2\cos x - \sqrt{3}} > 0$	$2k\pi \leq x < \frac{\pi}{6} + 2k\pi \vee \frac{2}{3}\pi + 2k\pi < x < \pi + 2k\pi \vee \frac{5}{3}\pi + 2k\pi < x < \frac{11}{6}\pi + 2k\pi$
6	$\frac{1-\cos x}{\cos 2x} \geq 0$	$-\frac{\pi}{4} + k\pi \leq x \leq \frac{\pi}{4} + k\pi$
7	$\frac{3\tan x - \sqrt{3}}{2\sin x - 1} \geq 0$	$(2k\pi \leq x < \frac{\pi}{2} + 2k\pi \wedge x \neq \frac{\pi}{6} + 2k\pi) \vee \frac{5}{6}\pi + 2k\pi < x \leq \frac{7}{6}\pi + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x \leq 2\pi + 2k\pi$
8	$\frac{2\cos x + \sqrt{3}}{\tan x - 1} < 0$	$(2k\pi \leq x < \frac{\pi}{2} + 2k\pi \wedge x \neq \frac{\pi}{4} + 2k\pi) \vee \frac{7}{6}\pi + 2k\pi < x < \frac{5}{4}\pi + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x \leq \pi + 2k\pi$
9	$\frac{2\sin x - \sqrt{3}}{\sin x + 1} > 0$	$\frac{\pi}{3} + 2k\pi < x < \frac{2}{3}\pi + 2k\pi$
10	$\frac{\sqrt{2} - 2\cos x}{2\sin x - \sqrt{2}} < 0$	$\frac{3}{4}\pi + k\pi < x < \frac{7}{4}\pi + 2k\pi$
11	$\frac{1-\sin x}{1-2\cos 2x} \geq 0$	$\frac{\pi}{6} + k\pi < x < \frac{5}{6}\pi + k\pi$
12	$\frac{\sqrt{3}-\cot x}{3\cot x - \sqrt{3}} \geq 0$	$\frac{\pi}{6} + k\pi \leq x < \frac{\pi}{3} + k\pi$
13	$\frac{1+\sqrt{2}\cos(x+\frac{\pi}{6})}{\sin x} \leq 0$	$\frac{7}{12}\pi + 2k\pi \leq x < \pi + 2k\pi \vee \frac{13}{12}\pi + 2k\pi \leq x < 2\pi + 2k\pi$

## Disequazioni goniometriche fratte

14	$\frac{\sin(x + \frac{\pi}{4})}{\sqrt{3} - 2 \cos x} > 0$	$\frac{\pi}{6} + 2k\pi < x < \frac{3}{4}\pi + 2k\pi \vee \frac{7}{4}\pi + 2k\pi < x < \frac{11}{6}\pi + 2k\pi$
15	$\frac{2 \cos(x - \frac{\pi}{3}) + \sqrt{3}}{2 \cos x - 1} < 0$	$\frac{\pi}{3} + 2k\pi < x < \frac{7}{6}\pi + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x < \frac{5}{3}\pi + 2k\pi$
16	$\frac{1 - \sin(x - \frac{\pi}{4})}{\cos x + 1} \geq 0$	$x \neq \pi + 2k\pi$
17	$\frac{1}{1 - \sin x} > 2$	$\frac{\pi}{6} + 2k\pi < x < \frac{5}{6}\pi + 2k\pi \wedge x \neq \frac{\pi}{2} + 2k\pi$
18	$\frac{\tan^2 x - \tan x}{4 \sin^2 x - 1} > 0$	$2k\pi < x < \frac{\pi}{6} + 2k\pi \vee \frac{\pi}{4} + 2k\pi < x < \frac{\pi}{2} + 2k\pi \vee \frac{5}{6}\pi + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
19	$\frac{\cot x}{1 - \tan^2 x} < 0$	$\frac{\pi}{4} + k\pi < x < \frac{\pi}{2} + k\pi \vee \frac{3}{4}\pi + k\pi < x < \pi + k\pi$
20	$\frac{\sin x}{1 + \sin x} > 2$	$\emptyset$
21	$\frac{2 \cos \frac{x}{2} - 1}{1 + \sin x} > 0$	$-\frac{2}{3}\pi + 4k\pi < x < \frac{2}{3}\pi + 4k\pi \wedge x \neq \frac{3}{2}\pi + 4k\pi$
22	$\frac{2 \cos^2 x - \cos x}{\sin x} > 0$	$2k\pi < x < \frac{\pi}{3} + 2k\pi \vee \frac{\pi}{2} + 2k\pi < x < \pi + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x < \frac{5}{3}\pi + 2k\pi$
23	$\frac{3 - 4 \cos^2 x}{2 \sin 2x - \sqrt{2}} < 0$	$\frac{\pi}{8} + k\pi < x < \frac{\pi}{6} + k\pi \vee \frac{3}{8}\pi + k\pi < x < \frac{5}{6}\pi + k\pi$
24	$\frac{\sin x - 2 \sin^2 x}{2 \sin x - 1} \leq 0$	$2k\pi \leq x \leq \pi + 2k\pi \wedge x \neq \frac{\pi}{6} + 2k\pi \wedge x \neq \frac{5}{6}\pi + 2k\pi$
25	$\frac{\sin^2 x + 2 \cos x - 2}{3 - \cos^2 x - \sin x} \geq 0$	$x = 2k\pi$
26	$\frac{\cos x - \frac{1}{2}}{2 \sin^2 x - 1} \leq 0$	$-\frac{\pi}{4} + 2k\pi < x < \frac{\pi}{4} + 2k\pi \vee \frac{\pi}{3} + 2k\pi \leq x < \frac{3}{4}\pi + 2k\pi \vee \frac{5}{4}\pi + 2k\pi < x \leq \frac{5}{3}\pi + 2k\pi$

## Disequazioni goniometriche fratte

27	$\frac{\sqrt{3} \sin x + \cos x}{\cos^2 x - \cos x} \leq 0$	$2k\pi < x < \frac{\pi}{2} + 2k\pi \vee \frac{5}{6}\pi + 2k\pi \leq x < \frac{3}{2}\pi + 2k\pi \vee \frac{11}{6}\pi + 2k\pi \leq x < 2\pi + 2k\pi$
28	$\frac{4 \sin^2 x - 11 \sin x + 3 + 2(1 - \sin^2 x)}{\cos x} \geq 0$	$-\frac{\pi}{2} + 2k\pi < x \leq \frac{\pi}{6} + 2k\pi \vee \frac{\pi}{2} + 2k\pi < x \leq \frac{5}{6}\pi + 2k\pi$
29	$\frac{2 \sin x - \sin x \cos x}{\tan x} \leq 1$	$x \neq k\pi$
30	$\frac{\cos x + \frac{\sqrt{3}}{2}}{\sin x \cos x + \sin x} \geq 0$	$2k\pi < x \leq \frac{5}{6}\pi + 2k\pi \vee \pi + 2k\pi < x \leq \frac{7}{6}\pi + 2k\pi$
31	$\frac{\sin x (2 \sin x - 1)}{2 \cos^2 x} \geq 0$	$\left(\frac{\pi}{6} + 2k\pi \leq x \leq \frac{5}{6}\pi + 2k\pi \wedge x \neq \frac{\pi}{2} + 2k\pi\right) \vee \left(\pi + 2k\pi \leq x \leq 2\pi + 2k\pi \wedge x \neq \frac{3}{2}\pi + 2k\pi\right)$
32	$\frac{2 \sin x \cos x + \sin x}{\sin x + \cos x} \leq 0$	$\frac{2}{3}\pi + 2k\pi \leq x < \frac{3}{4}\pi + 2k\pi \vee \pi + 2k\pi \leq x \leq \frac{4}{3}\pi + 2k\pi \vee \frac{7}{4}\pi + 2k\pi < x \leq 2\pi + 2k\pi$
33	$\frac{4 \sin x}{3 - 4 \sin^2 x} \leq 0$	$\frac{\pi}{3} + 2k\pi < x < \frac{2}{3}\pi + 2k\pi \vee \pi + 2k\pi \leq x < \frac{4}{3}\pi + 2k\pi \vee \frac{5}{3}\pi + 2k\pi < x \leq 2\pi + 2k\pi$
34	$\frac{\sin x + 1}{\tan^2 x} \geq -1$	$\forall x \in \mathbb{R}$
35	$\frac{\sin x (2 \sin x + 1)}{\frac{\cos^2 x - \sin^2 x}{\cos^2 x}} \geq 0$	$2k\pi \leq x < \frac{\pi}{4} + 2k\pi \vee \frac{3}{4}\pi + 2k\pi < x \leq \pi + 2k\pi \vee \frac{7}{6}\pi + 2k\pi \leq x < \frac{5}{4}\pi + 2k\pi \vee \frac{7}{4}\pi + 2k\pi < x \leq \frac{11}{6}\pi + 2k\pi \vee \frac{\pi}{2} + k\pi$
36	$\frac{\cos x}{1 + \cos x} > \tan^2 \frac{x}{2}$	$-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{3} + 2k\pi$
37	$\frac{\sin \left(\frac{\pi}{2} - x\right)}{1 + \cos \left(\frac{\pi}{2} - x\right)} > 2 - \cot \left(\frac{\pi}{2} - x\right)$	$\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{2} + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x < \frac{5}{3}\pi + 2k\pi$
38	$\frac{\sqrt{3} \sin x + \cos x (\cos x - 1)}{\cos^2 x} \leq 1$	$-\frac{5}{6}\pi + 2k\pi \leq x \leq \frac{\pi}{6} + 2k\pi \wedge x \neq \frac{3}{2}\pi + 2k\pi$

# Disequazioni goniometriche fratte

39	$\frac{\sin 2x - \tan x}{\cos^2 x + 3 \sin^2 x} \leq 0$	$\frac{\pi}{4} + k\frac{\pi}{2} \leq x < \frac{\pi}{2} + k\frac{\pi}{2}$
40	$\frac{1 - \sin x - 2 \cos x}{\cos x} > -\tan x$	$\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{2} + 2k\pi \vee \frac{3}{2}\pi + 2k\pi < x < \frac{5}{3}\pi + 2k\pi$
41	$\frac{4 \cos^2 \frac{x}{2} - 2 \sin^2 \frac{x}{2} - \cos x - 2}{1 - \sin^2 x} \geq 0$	$2k\pi \leq x \leq \frac{\pi}{3} + 2k\pi \vee \\ \frac{5}{3}\pi + 2k\pi \leq x \leq 2\pi + 2k\pi$
42	$\frac{\cos(\frac{\pi}{4} - x)}{4\tan x - (1 - 3\tan x)} < 0$	$-\frac{\pi}{4} + 2k\pi \leq x < \frac{\pi}{4} + 2k\pi \vee \\ \frac{\pi}{2} + 2k\pi < x < \frac{3}{4}\pi + 2k\pi \vee \\ \frac{5}{4}\pi + 2k\pi < x < \frac{3}{2}\pi + 2k\pi$
43	$\frac{4\cot^2 x - 3(1 + \cot^2 x)}{2\cos^2 x - 1} \geq 0$	$\left(-\frac{\pi}{6} + k\pi \leq x \leq \frac{\pi}{6} + k\pi \wedge x \neq \pi + k\pi\right) \vee \\ \frac{\pi}{4} + k\pi < x < \frac{3}{4}\pi + k\pi$
44	$\frac{(\cos x + 1)(2 \sin x + 1)}{\cos x - \frac{\sqrt{3}}{3} \sin x} < 0$	$\frac{\pi}{3} + 2k\pi < x < \frac{7}{6}\pi + 2k\pi \vee \\ \frac{4}{3}\pi + 2k\pi < x < \frac{11}{6}\pi + 2k\pi \wedge \\ x \neq \pi + 2k\pi$
45	$\frac{\sin 2x (3 - 4 \sin^2 x)}{\sin x} \geq 0$	$2k\pi < x \leq \frac{\pi}{3} + 2k\pi \vee \frac{\pi}{2} + 2k\pi \leq x \leq \frac{2}{3}\pi + 2k\pi \vee \\ \frac{4}{3}\pi + 2k\pi \leq x \leq \frac{3}{2}\pi + 2k\pi \vee \\ \frac{5}{3}\pi + 2k\pi \leq x < 2\pi + 2k\pi$
46	$\frac{ \sin x }{6\cos x + 3 - 4(\cos x + 1)} \geq 0$	$-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{3} + 2k\pi$
47	$\frac{ \cos x  + 1}{4\sin x - 2\sqrt{3}} < 0$	$2k\pi \leq x < \frac{\pi}{3} + 2k\pi \vee \frac{2}{3}\pi + 2k\pi < x \leq 2\pi + 2k\pi \\ x \neq \pi + 2k\pi$
48	$\frac{2\sin^2 x - 1}{ \cos x } > \tan x$	$\frac{\pi}{2} + 2k\pi < x < \frac{5}{6}\pi + 2k\pi \vee \\ \frac{3}{2}\pi + 2k\pi < x < \frac{11}{6}\pi + 2k\pi$
49	$\frac{\sin x - \cos x}{\sin x + \cos x} < 0$	$2k\pi < x < \frac{\pi}{4} + 2k\pi ; \frac{3}{4}\pi + 2k\pi < x < \frac{5}{4}\pi + 2k\pi ; \\ \frac{7}{4}\pi < x < 2(k+1)\pi$
50	$\frac{\sin x}{1 - 2\sin x} > 0$	$2k\pi < x < \frac{\pi}{6} + 2k\pi ; \frac{5}{6}\pi + 2k\pi < x < \pi + 2k\pi ;$

## Disequazioni goniometriche fratte

51	$\frac{\cos 2x + \cos x - 1}{\cos 2x} > 2$	$-\frac{3}{4}\pi + 2k\pi < x < -\frac{\pi}{2} + 2k\pi;$ $-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{4} + 2k\pi;$ $\frac{\pi}{4} < x < \frac{\pi}{3} + 2k\pi; \frac{\pi}{2} + 2k\pi < x < \frac{3}{4}\pi + 2k\pi$
52	$\left  \frac{\cos 2x}{\sin x} \right  < 1; x \in [0, 2\pi]$	$\frac{\pi}{6} < x < \frac{\pi}{2}; \frac{\pi}{2} < x < \frac{5}{6}\pi;$ $\frac{7}{6}\pi < x < \frac{3}{2}\pi; \frac{3}{2}\pi < x < \frac{11}{6}\pi$
53	$\frac{(x-1)\sin x}{(x+2)^2} > 0$	$1 < x < \pi; 2k\pi < x < 2(k+1)\pi, k \in \mathbb{Z} \wedge k \geq 1;$ $2(k-1)\pi < x < 2k\pi, k \in \mathbb{Z}^- \wedge x \neq 2$
54	$\frac{\sin x + \cos x}{\tan x - 1} \geq 0$	$\frac{\pi}{4} + 2k\pi < x < \frac{\pi}{2} + 2k\pi;$ $\frac{3}{4}\pi + 2k\pi \leq x < \frac{5}{4}\pi + 2k\pi;$ $\frac{3}{2}\pi + 2k\pi < x \leq \frac{7}{4}\pi + 2k\pi$
55	$\frac{\sin x + \cos x}{\tan x - \cot x} > 0$	$\frac{\pi}{4} + 2k\pi < x < \frac{\pi}{2} + 2k\pi;$ $\pi + 2k\pi < x < \frac{5}{4}\pi + 2k\pi;$ $\frac{3}{2}\pi + 2k\pi < x < 2\pi + 2k\pi$
56	$\frac{\cos x}{\sqrt{2\cos x - 1}} > \frac{1}{\sqrt{2}};$	$-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{3} + 2k\pi$
57	$\tan \frac{1}{x^2 + 1} \geq 1$	$-\sqrt{\frac{4-\pi}{\pi}} \leq x \leq \sqrt{\frac{4-\pi}{\pi}}$
58	$\frac{2\tan \frac{x}{2} + \frac{\sin x}{1+\cos x} - \sqrt{3}}{1-\sin x} > 0$	$\frac{\pi}{3} + 2k\pi < x < \pi + 2k\pi \wedge x \neq \frac{\pi}{2} + 2k\pi$
59	$\frac{4\tan x - \frac{1}{\cos^2 x}}{ 16x^2 - 24\pi x + 5\pi^2 } > 0$	$\frac{\pi}{12} + k\pi < x < \frac{5}{12}\pi + k\pi \wedge x \neq \frac{\pi}{4} \wedge x \neq \frac{5}{4}\pi$
60	$\left  \frac{\tan 2x}{\cot x} \right  < 1$	$-\frac{\pi}{6} + k\pi < x < \frac{\pi}{6} + k\pi$
61	$\frac{\cos 2\sqrt{x} - \sin \sqrt{x}}{\sin 2\sqrt{x} - \cos \sqrt{x}} > 0, x \in [0, 4\pi^2]$	$\frac{\pi^2}{36} < x < \frac{\pi^2}{9}; \frac{25}{36}\pi \leq x \leq \pi^2; \frac{25}{9}\pi^2 \leq x \leq 4\pi^2$
62	$\frac{4\sin^2 x - 3}{\sin x} > 2 \frac{\cos x}{ \sin x }$	$\frac{2}{5}\pi + 2k\pi < x < \frac{4}{5}\pi + 2k\pi;$ $-\pi + 2k\pi < x < -\frac{3}{5}\pi + 2k\pi;$ $-\frac{1}{5}\pi + 2k\pi < x < 2k\pi$

## Disequazioni goniometriche fratte

63	$\frac{1 - \sin x}{1 - 2\sin x} < \frac{1 + \sin x}{1 - 4\sin^2 x}$	$2k\pi < x < \frac{\pi}{6} + 2k\pi ; \frac{5}{6}\pi + 2k\pi < x < \pi + 2k\pi;$ $\pi + 2k\pi < x < \frac{7}{6}\pi + 2k\pi;$ $\frac{11}{6}\pi + 2k\pi < x < 2\pi + 2k\pi$
64	$\frac{1 +  \sin x }{\tan x} < 0$	$-\frac{\pi}{2} + k\pi < x < k\pi$
65	$\frac{\sqrt{2} \tan x}{1 - \sin^3 x} > 0$	$k\pi < x < \frac{\pi}{2} + k\pi$
66	$\frac{\sqrt{3} \cot x}{\cos(2x)} > 0$	$k\pi < x < \frac{\pi}{4} + k\pi ; -\frac{\pi}{2} + k\pi < x < -\frac{\pi}{4} + k\pi$
67	$\frac{\tan^2 2x}{\cot 2x} > 0$	$k\pi < x < \frac{\pi}{4} + k\pi ; -\frac{\pi}{2} + k\pi < x < -\frac{\pi}{4} + k\pi$
68	$\frac{\sqrt{\sin x}}{ \cos(2x) } > 0$	$\frac{\pi}{4} + 2k\pi < x < \frac{3}{4}\pi + 2k\pi ; 2k\pi < x < \frac{\pi}{4} + 2k\pi$ $\frac{3}{4}\pi + 2k\pi < x < \pi + 2k\pi$
69	$\frac{-\cos^2 x - 3}{2\cos^2 x} > \frac{\cos x}{1 - 2\cos^2 x}$	$\frac{\pi}{4} + k\pi < x < \frac{3}{4}\pi + k\pi$
70	$\frac{\sin^2 x - 2}{\cos x} < 0$	$-\frac{\pi}{2} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
71	$\frac{1 +  2\sin x }{1 + 2\sin x} > 0$	$2k\pi \leq x < \frac{7}{6}\pi + 2k\pi \quad \vee$ $\frac{11}{6}\pi + 2k\pi < x < \pi + 2k\pi$
72	$\frac{1 - 2 \sin x }{1 + \sin x} > 0$	$-\frac{\pi}{6} + 2k\pi < x < \frac{\pi}{6} + 2k\pi \quad \vee$ $\frac{5}{6}\pi + 2k\pi < x < \frac{7}{6}\pi + 2k\pi$
73	$\frac{2 + \cos^2 x + \cot^2 x}{\cos x + \sin x} < 1$	$-\pi + 2k\pi < x < -\frac{\pi}{4} + 2k\pi$ $\frac{3}{4}\pi + 2k\pi < x < \pi + 2k\pi$
74	$\frac{2 \sin x  - 1}{2\sin x - 1} > 0 \quad [0 \leq x \leq 2\pi]$	$0 \leq x < \frac{7}{6}\pi \quad \vee \quad \frac{11}{6}\pi < x \leq 2\pi$ $\wedge \quad x \neq \frac{\pi}{6} \quad \wedge \quad x \neq \frac{5}{6}\pi$
75	$\frac{2\sin x + \sqrt{3}}{ \cos x } \leq 0$	$\frac{4}{3}\pi + 2k\pi < x < \frac{3}{2}\pi + 2k\pi \quad \vee$ $\frac{2}{3}\pi + 2k\pi < x \leq \frac{5}{3}\pi + 2k\pi$

## Disequazioni goniometriche fratte

76	$\frac{2 \sin x + 1}{1 - \sin x} \geq 0$	$x \neq \frac{\pi}{2} + 2\kappa\pi$
77	$\frac{1 - 2 \sin x }{2 \sin x + 1} > 0 \quad [0 < x < 2\pi]$	$0 < x \frac{\pi}{6} \vee \frac{5}{6}\pi < x < 2\pi \wedge x \neq \frac{7}{6}\pi \wedge x \neq \frac{11}{6}\pi$
78	$\frac{\tan x - 3}{\sin x} < 0 \quad [0 \leq x \leq 2\pi]$	$0 < x < \frac{\pi}{3} \vee \frac{2}{3}\pi < x < \frac{4}{3}\pi \quad x \neq \frac{3}{2}\pi$
79	$\frac{2 \sin x  + \sqrt{3}}{\cos x} > 0$	$-\frac{\pi}{2} + 2\kappa\pi < x < \frac{\pi}{2} + 2\kappa\pi$
80	$\frac{1 -  2 \sin x }{1 + \sin x} > 0$	$-\frac{\pi}{6} + 2\kappa\pi < x < \frac{\pi}{6} + 2\kappa\pi \vee \\ \frac{5}{6}\pi + 2\kappa\pi < x < \frac{7}{6} + 2\kappa\pi$
81	$\frac{1 - 3 \cot^2 x}{2 \cos x - 1} < 0 \quad [0 < x < 2\pi]$	$0 < x < \frac{2}{3}\pi \vee \frac{4}{3}\pi < x < 2\pi \\ \wedge x \neq \frac{5}{3}\pi \wedge x \neq \frac{\pi}{3}$
82	$\frac{\sin 5x + \sin 3x}{\sin 4x} > 0$	$-\frac{\pi}{2} + 2\kappa\pi < x < \frac{\pi}{2} + 2\kappa\pi \wedge \\ x \neq \frac{\pi}{4} + 2\kappa\pi \wedge x \neq 2\kappa\pi$
83	$\frac{3 \tan x + \sqrt{3}}{\cot x + \sqrt{3}} (2 \sin x - 1) < 0$	$2\kappa\pi < x < \frac{\pi}{6} + 2\kappa\pi \vee \\ \frac{\pi}{2} + 2\kappa\pi < x < \frac{5}{6}\pi + 2\kappa\pi \vee \\ \pi + 2\kappa\pi < x < \frac{3}{2}\pi + 2\kappa\pi$
84	$\frac{\sin x}{1 + \cos x} > 2 - \cot x$	$2\kappa\pi < x < 2\kappa\pi + \frac{\pi}{6} \vee \\ \frac{5}{6} + 2\kappa\pi < x < \pi + 2\kappa\pi$
85	$\frac{4 \cos^2 x - 1}{\cos x} < 0$	$\frac{\pi}{3} + 2\kappa\pi < x < \frac{\pi}{2} + 2\kappa\pi \vee \\ \frac{2}{3}\pi + 2\kappa\pi < x < \frac{4}{3}\pi + 2\kappa\pi \vee \\ \frac{3}{2}\pi + 2\kappa\pi < x < \frac{5}{3}\pi + 2\kappa\pi$
86	$\frac{3 \sin x - \sqrt{3} \cos x}{2 \cos x - 1} \leq 0$	$-\frac{\pi}{3} + 2\kappa\pi < x \leq \frac{\pi}{6} + 2\kappa\pi \vee \\ \frac{\pi}{3} + 2\kappa\pi < x \leq \frac{7}{6}\pi + 2\kappa\pi$
87	$\frac{\cos 7x - \cos 3x}{\sin x \cos x} > 0$	$\frac{\pi}{5}(1 + 2\kappa) < x < \frac{2}{5}\pi(1 + 2\kappa) \wedge \\ x \neq 2\kappa\pi$
88	$\frac{\sin x}{2 \sin x \frac{\pi}{4} + \cos x} > 0$	$2\kappa\pi < x < \pi + 2\kappa\pi$

## Disequazioni goniometriche fratte

89	$\frac{2 \sin x - 1}{2 \sin x + 1} < 0$	$-\frac{\pi}{6} + \kappa\pi < x < \frac{\pi}{6} + \kappa\pi$
90	$\frac{\sin^2 x + \cos^2 x}{\sin x - \cos x} > 0$	$\frac{\pi}{4} + 2\kappa\pi < x < \frac{5}{4}\pi + 2\kappa\pi$
91	$\frac{\tan x - \tan \frac{\pi}{3}}{1 - 2 \cos x} > 0$	$-\frac{\pi}{3} + 2\kappa\pi < x < \frac{\pi}{2} + 2\kappa\pi \text{ con } x \neq \frac{\pi}{3} + 2\kappa\pi;$ $\frac{4}{3}\pi + 2\kappa\pi < x < \frac{3}{2}\pi + 2\kappa\pi$
92	$\frac{\sin x \cos x}{2 \cos^2 x - 1} \geq 0$	$0 \leq x < \frac{\pi}{4} \vee \frac{\pi}{2} \leq x < \frac{3}{4}\pi \vee$ $\pi \leq x < \frac{5}{4}\pi \vee \frac{3}{2}\pi \leq x < \frac{7}{4}\pi$