

# Espressioni goniometriche

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Gli esercizi sono proposti in ordine di difficoltà crescente.

**nota:** in un file così lungo e complesso può accadere che sia presente un errore di diversa natura nonostante gli esercizi siano stati controllati più volte. Saremo grati di ricevere segnalazioni di eventuali refusi o suggerimenti di qualsiasi natura.

## 1. espressioni con angoli notevoli

1	$\sin 0^\circ \cos 90^\circ + 2 \cos 180^\circ$	-2
2	$5 \tan 180^\circ + \sin 90^\circ + 2 \cos 270^\circ$	1
3	$1 - \cos 180^\circ + \cos 360^\circ + 2 \sin 90^\circ$	5
4	$15 \cos 180^\circ + 14 \cos 0^\circ + \cos 360^\circ$	0
5	$\sin 180^\circ - 4 \cos 90^\circ + 3 \sin 270^\circ$	-3
6	$4 \cos 270^\circ + \sin 90^\circ + \sin 180^\circ - \tan 180^\circ$	1
7	$\cos 180^\circ + \sin 90^\circ + 3 \sin 180^\circ - \tan 0^\circ$	0
8	$20 \sin 270^\circ + 12 \cos 180^\circ - (\sin 270^\circ + 1)$	-32
9	$3 \cos 0^\circ - 7 \sin 180^\circ \cos 270^\circ + \tan 360^\circ$	3
10	$3 \cos 0^\circ - 2 \sin \frac{3}{2}\pi - \left( 5 \sin \frac{\pi}{2} + 3 \cos \pi \right) + 2 \cos 0^\circ$	5
11	$5 \cos \frac{3}{2}\pi - 2 \left( \sin \pi - 4 \cos \frac{\pi}{2} + 3 \cos \pi \right) + 2 \cos \frac{3}{2}\pi$	6
12	$\sin 2\pi - \left( 4 \sin \frac{\pi}{2} + 3 \cos \pi \right) + 3 \tan \pi + 2 \cos \frac{3}{2}\pi$	-1

13	$\frac{1}{2} \left( \sin \frac{\pi}{2} + \frac{2}{3} \sin \frac{3}{2}\pi \right) - \frac{1}{3} \cos \pi$	$\frac{1}{2}$
14	$\cos \frac{3}{2}\pi - \frac{2}{5} \left( \sin 2\pi - \sin \frac{\pi}{2} \right) - \frac{1}{10} \cos \pi$	$\frac{1}{2}$
15	$\left( 2 \sin \frac{3}{2}\pi - 5 \cos \pi \right)^2 - 4$	5
16	$\left( \frac{1}{3} \sin \frac{\pi}{2} \right)^2 - 4 \tan 2\pi - \frac{1}{9} \cos 0 \cos \frac{3}{2}\pi$	$\frac{1}{9}$
17	$\left( \sin 360^\circ + \frac{1}{2} \cos 180^\circ \right) \cot 90^\circ$	0
18	$\left( \tan 0^\circ - \frac{1}{3} \sin 270^\circ \right)^{\frac{1}{2}}$	$\frac{\sqrt{3}}{3}$
19	$(\sec 180^\circ + \csc 90^\circ)(1 + \cos 0^\circ)$	0
20	$\frac{\cos 270^\circ + \tan 180^\circ}{3 \csc 90^\circ}$	0
21	$\sin^2 90^\circ + \cos^2 360^\circ$	2

22	$(\tan \pi + \cot \frac{\pi}{2}) \cos 0$	0
23	$\frac{\cos \pi + \frac{1}{2} \cos \frac{\pi}{2}}{2 \sin \frac{3}{2}\pi}$	$\frac{1}{2}$
24	$\sec \pi (\sin^2 2\pi + \cos 0)$	-1
25	$\sec 0 \sin \pi + \sqrt{5} \sin \frac{\pi}{2}$	$\sqrt{5}$
26	$\frac{1 + \tan \pi}{\csc \frac{\pi}{2}}$	1
27	$\cos 45^\circ - \cos 30^\circ + \sin 60^\circ$	$\frac{\sqrt{2}}{2}$
28	$\sin 30^\circ - \tan 45^\circ + \cos 60^\circ$	0
29	$\sin 60^\circ - \cos 30^\circ + \tan 30^\circ$	$\frac{\sqrt{3}}{3}$
30	$\tan 60^\circ - 2\sin 45^\circ + 3\tan 30^\circ$	$2\sqrt{3} - \sqrt{2}$

31	$\sin \frac{\pi}{3} \cos \pi + \sin \frac{\pi}{6} + \frac{\sqrt{3}}{2}$	$\frac{1}{2}$
32	$\sqrt{3} - \sin \frac{3}{2}\pi - \tan \frac{\pi}{4} - \tan \frac{\pi}{3}$	0
33	$\sin 45^\circ \cos 180^\circ + \frac{\sqrt{2}}{2} + 2 \sin 60^\circ$	$\sqrt{3}$
34	$\sin 45^\circ \cos 180^\circ - \cos 45^\circ \sin 270^\circ$	0
35	$2 \cos 60^\circ - 3 \sin 180^\circ + 8 \cos 30^\circ + 3 \tan 30^\circ$	$1 + 5\sqrt{3}$
36	$6 \tan 30^\circ - 3 \tan 60^\circ + 2 \cos 30^\circ + 4 \sin 60^\circ$	$2\sqrt{3}$
37	$\cos 30^\circ - \sin 60^\circ + 4(\cos 45^\circ + \sin 45^\circ)$	$4\sqrt{2}$
38	$\sin \frac{3}{2}\pi \cos \frac{\pi}{6} + \cos \frac{\pi}{2} \sin \frac{\pi}{3}$	$-\frac{\sqrt{3}}{2}$
39	$\sin \frac{\pi}{3} \cos \frac{\pi}{6} + \sqrt{3} \tan \frac{\pi}{3}$	$\frac{15}{4}$
40	$\sin \frac{\pi}{6} \cos \frac{\pi}{3} - 4 \cos \frac{\pi}{4} \tan \frac{\pi}{3} + 2\sqrt{6}$	$\frac{1}{4}$
41	$(4 \sin 30^\circ + \sqrt{2} \tan 45^\circ) \left(1 + \frac{1}{3} \cos 30^\circ\right)$	$(2 + \sqrt{2}) \left(1 + \frac{\sqrt{3}}{6}\right)$

42	$4 \cos 45^\circ \sin^2 60^\circ$	$\frac{3}{2}\sqrt{2}$
43	$(\sin 60^\circ + \cot^2 45^\circ) \frac{1}{\sin 30^\circ}$	$\sqrt{3} + 2$
44	$1 - \sin 45^\circ \cos 45^\circ$	$\frac{1}{2}$
45	$\tan^2 30^\circ \sin^2 60^\circ$	$\frac{1}{4}$
46	$\left(\sin \frac{\pi}{3} + \cos \frac{\pi}{6}\right) \frac{1}{\tan \frac{\pi}{3}}$	1
47	$\left(\sqrt{3} \cos \frac{\pi}{6} + \sin \frac{\pi}{6}\right) \cot^2 \frac{\pi}{4}$	2
48	$\sqrt{2} \cos \frac{\pi}{4} + 2\sqrt{3} \sin \frac{\pi}{3}$	4
49	$csc \frac{\pi}{4} \frac{1}{sec \frac{\pi}{3}}$	$\frac{\sqrt{2}}{2}$
50	$\frac{3 \tan \frac{\pi}{6} + \tan \frac{\pi}{3}}{\tan \frac{\pi}{4}}$	$2\sqrt{3}$

## letterali

51	$\frac{a \csc^2 90^\circ + b \sec^2 0^\circ}{a \sin 270^\circ}$	$-\frac{a+b}{a}$
52	$(2a \cos 180^\circ)^2 + (2b \cos 270^\circ)^2$	$4a^2$
53	$\left(\frac{\sqrt{a} \sec 0^\circ}{a \cos 180^\circ}\right) \sin 270^\circ$	$\frac{\sqrt{a}}{a}$
54	$\frac{b - \cos 90^\circ}{\sin 270^\circ} - \frac{a}{\sec 0^\circ}$	$-(a+b)$
55	$\sqrt[3]{a} \tan 0^\circ - \frac{b}{\cot^2 90^\circ - 1}$	$b$
56	$(\tan^2 \pi + a) \cos 0 + \sin \frac{3}{2}\pi$	$a - 1$
57	$\frac{a \cos \pi + \sin \frac{\pi}{2}}{a \csc \frac{3}{2}\pi + b \sec \pi}$	$\frac{a-1}{a+b}$
58	$\frac{4a\sqrt{3} \sin \frac{3}{2}\pi - b \cos \frac{\pi}{2}}{a \csc \frac{3}{2}\pi}$	$4\sqrt{3}$
59	$b \cos 2\pi (\sec 0 + a \tan 2\pi)$	$b$

60	$\sec 2\pi \tan^2 \pi + 3a \sin \frac{3}{2}\pi$	-3a
61	$\sqrt{2ab(\sin^2 30^\circ + \cot 45^\circ)}$	$\frac{\sqrt{10ab}}{2}$
62	$\frac{3}{2}a \csc 60^\circ(b \cos 45^\circ - c \tan 30^\circ)$	$\frac{\sqrt{6}ab}{2} - ac$
63	$\sqrt{a} \cot 45^\circ + \frac{b \sin 45^\circ}{1 + c \tan 30^\circ}$	$\sqrt{a} + \frac{3}{2}\sqrt{2} \frac{b}{3 + \sqrt{3}c}$
64	$\frac{b^2 \csc^2 60^\circ}{\sin 30^\circ} + \frac{a}{\sec^2 60^\circ}$	$\frac{8}{3}b^2 + \frac{a}{4}$
65	$\frac{2a + \sin 45^\circ}{b \cos 60^\circ} \cot 30^\circ$	$\frac{2\sqrt{3}}{b} \left(2a + \frac{\sqrt{2}}{2}\right)$
66	$\frac{\sqrt{a} \sin \frac{\pi}{3} \sqrt{b} \tan \frac{\pi}{4}}{c \csc \frac{\pi}{6}}$	$\frac{\sqrt{3ab}}{4c}$
67	$\left(a \tan \frac{\pi}{3} - b \cot \frac{\pi}{6}\right) b \csc^2 \frac{\pi}{4}$	$2\sqrt{3}b(a - b)$
68	$\left(1 - a \sin \frac{\pi}{4} - b \sin \frac{\pi}{6} \tan^2 \frac{\pi}{4}\right)^{\frac{1}{3}}$	$\left(1 - \frac{a\sqrt{2}}{2} - \frac{b}{2}\right)^{\frac{1}{3}}$
69	$\frac{\sqrt{2a} \csc \frac{\pi}{4}}{1+b \sec \frac{\pi}{3}} b \cot \frac{\pi}{4}$	$\frac{2b\sqrt{a}}{1+2b}$

70	$\left(a \cos^2 \frac{\pi}{4} + b \sin \frac{\pi}{6}\right) c \csc \frac{\pi}{3}$	$\left(\frac{a+b}{\sqrt{3}}\right)c$
2. espressioni con angoli superiori a $360^\circ$		
71	$2\sin 450^\circ + \cos 630^\circ$	2
72	$\frac{1}{3}\cos 720^\circ - 2\cos 540^\circ$	$\frac{7}{3}$
73	$1 - 2(\cos 720^\circ - \sin 900^\circ)$	-1
74	$\sin 420^\circ - \cos 390^\circ - \frac{1}{4}\cos 540^\circ$	$\frac{1}{4}$
75	$\sin 450^\circ - \cos 540^\circ - 2\sin 630^\circ$	4
76	$\sqrt{2}\sin 405^\circ - \sqrt{3}\cos 390^\circ$	$-\frac{1}{2}$
77	$\sin 630^\circ - \tan 720^\circ + 1$	0
78	$\sin 540^\circ \cos 450^\circ - \tan 540^\circ$	0
79	$\sin 6\pi - 3\left(\sin \frac{7}{2}\pi - \cos \frac{9}{2}\pi\right)$	3
80	$2\left(\sin \frac{9}{4}\pi - 3\cos \frac{5}{2}\pi\right)$	$\sqrt{2}$

81	$(\cos 360^\circ + 2 \cos 450^\circ)(1 - \tan 540^\circ)$	1
82	$\sqrt{2} \sin 450^\circ + \tan^2 360^\circ$	$\sqrt{2}$
83	$\left(3 \tan 540^\circ + \frac{2}{5} \cot 450^\circ\right)^{\frac{\sqrt{2}}{2}}$	0
84	$\sin 630^\circ + \frac{\cos^2 540^\circ}{\sin 450^\circ}$	0
85	$\sec 360^\circ \csc 450^\circ + \sqrt{3} \tan 540^\circ$	1
86	$\left(\cos \frac{5}{2}\pi + \frac{1}{2} \cos 3\pi\right) \sin \frac{3}{2}\pi$	$\frac{1}{2}$
87	$\frac{\tan \pi + \cot \frac{\pi}{2}}{\cos 2\pi}$	0
88	$\frac{1}{10} \sec 3\pi \csc \frac{3}{2}\pi$	$\frac{1}{10}$
89	$\sqrt{3} \sin \frac{5}{2}\pi \frac{1}{3} \cos 2\pi$	$\frac{\sqrt{3}}{3}$
90	$\left(1 - \cos \frac{3}{2}\pi\right)(1 + \cos 2\pi)$	2
91	$2 \sin 390^\circ + \frac{\cos^2 390^\circ}{\sin 405^\circ}$	$\frac{4 + 3\sqrt{2}}{4}$

92	$\frac{1 - \cos 420^\circ}{1 + \cos 420^\circ} - \cot^2 390^\circ$	$-\frac{8}{3}$
93	$\tan 405^\circ(1 + \cot 390^\circ) - 1$	$\sqrt{3}$
94	$\frac{\sec 390^\circ}{1 + \tan^2 420^\circ} + \frac{1}{\csc 390^\circ}$	$\frac{\sqrt{3} + 3}{6}$
95	$\cot^2 420^\circ - \csc^2 390^\circ + \frac{1}{\sec 405^\circ}$	$\frac{3\sqrt{2} - 22}{6}$
96	$\left(\tan \frac{9}{4}\pi + 1\right) \sec \frac{7}{3}\pi$	4
97	$\left(\frac{\cos \frac{9}{4}\pi}{1 - \sin \frac{13}{6}\pi}\right) - \sin \frac{9}{4}\pi$	$\frac{\sqrt{2}}{2}$
98	$\frac{\cot^2 \frac{13}{6}\pi - \cos^2 \frac{7}{3}\pi}{\csc \frac{7}{3}\pi}$	$\frac{11}{8}\sqrt{3}$
99	$\cos \frac{9}{4}\pi + \frac{\sin^2 \frac{9}{4}\pi}{\cos \frac{7}{3}\pi}$	$\frac{2 + \sqrt{2}}{2}$
100	$\frac{\csc \frac{7}{3}\pi}{\sec \frac{7}{3}\pi} \tan \frac{9}{4}\pi$	$\frac{\sqrt{3}}{3}$

letterali		
101	$a\sqrt{3}(\cos^2 360^\circ + \cot 450^\circ)$	$\sqrt{3}a$
102	$\frac{\sec 360^\circ}{a} (\sqrt{a} \sin^2 540^\circ - b \cos^2 540^\circ)$	$-\frac{b}{a}$
103	$(\sin 630^\circ + a^2 \cos 630^\circ)^2$	1
104	$\frac{-b \cos 360^\circ - a \sin 630^\circ}{(a+b) \sec 540^\circ}$	$\frac{b-a}{a+b}$
105	$\sqrt{c} \left( \frac{\sqrt{3}}{2} a \sec 540^\circ + \frac{\sqrt{2}}{3} b \csc 450^\circ \right)$	$\frac{\sqrt{2c}}{3} b - \frac{\sqrt{3ca}}{2}$
106	$\left( a \cos 3\pi + \sin \frac{5}{2}\pi \right)^2 + \left( \cos \frac{5}{2}\pi - \sqrt{b} \sin \frac{7}{2}\pi \right)^2$	$b + (1-a)^2$
107	$\frac{a^2 \csc \frac{7}{2}\pi + b \sec 2\pi}{a \cos 3\pi - b^3 \sin 2\pi}$	$\frac{a^2 - b}{a}$
108	$\left( b^4 \tan 2\pi + a^6 \csc \frac{7}{2}\pi \right)^2 2ab \sin \frac{7}{2}\pi$	$-2a^{13}b$
109	$(1 + a \tan^2 3\pi) \sqrt{b} \sin \frac{5}{2}\pi$	$\sqrt{b}$
110	$\sin^2 390^\circ \frac{\sqrt{ab}}{\csc 420^\circ} + a \cot 405^\circ$	$\frac{\sqrt{3ab}}{8} + a$
111	$\frac{a \tan 420^\circ}{b - \cot 405^\circ} c \sec^2 390^\circ$	$\frac{4ac\sqrt{3}}{3(b-1)}$

112	$(\sin 420^\circ + a^3 \tan 405^\circ) \cot 405^\circ - 3a^3$	$\frac{\sqrt{3}}{2} - 2a^3$
113	$(\sqrt{a} \tan^2 420^\circ - 1) \sec^2 390^\circ + 1$	$\frac{4}{3}(3\sqrt{a} - 1) + 1$
114	$\left( \frac{(2b \tan 405^\circ)^2}{\cos^2 420^\circ} \right)^{\frac{1}{4}}$	$2\sqrt{b}$
115	$\left( 2a \tan^2 \frac{13}{6}\pi - 1 \right) b \cos^2 \frac{9}{4}\pi$	$\frac{b}{6}(2a - 3)$
116	$\left( 4b \sin \frac{13}{6}\pi + 6a \sin^2 \frac{9}{4}\pi \right) \frac{1}{\csc \frac{7}{3}\pi(a+b) \cot \frac{13}{6}\pi}$	$\frac{2b+3a}{2(a+b)}$
117	$\left( \frac{a + \sin \frac{9}{4}\pi - b \cos \frac{9}{4}\pi}{1 + \sin^2 \frac{9}{4}\pi + b \cos \frac{9}{4}\pi} \right)^{\frac{1}{2}}$	$\sqrt{\frac{2a + \sqrt{2}(1-b)}{3 + \sqrt{2}b}}$
118	$\frac{\left( b - 3 \cot^2 \frac{7}{3}\pi \right) \left( b \tan \frac{9}{4}\pi + 2 \cos \frac{7}{3}\pi \right)}{2b \csc \frac{13}{6}\pi - 1}$	$\frac{(b-1)(b+1)}{4b-1}$
119	$\frac{\sqrt{ab} \cos \frac{13}{6}\pi \left( 1 + a \sin^2 \frac{9}{4}\pi \right)^2}{\left( 2 \cot^2 \frac{9}{4}\pi + \frac{a}{2} \sec \frac{7}{3}\pi \right)^2}$	$\frac{\sqrt{3ab}}{8}$
<b>3. espressioni da risolvere con gli angoli associati</b>		1
120	$\sin 120^\circ + \cos 210^\circ$	0

121	$\cos 240^\circ - \sin 150^\circ$	-1
122	$\sin 120^\circ + \cos 225^\circ$	$\frac{\sqrt{3} - \sqrt{2}}{2}$
123	$\cos 210^\circ - \sin 330^\circ$	$\frac{1 - \sqrt{3}}{2}$
124	$\sin 315^\circ - \cos 240^\circ - \sin 135^\circ$	$\frac{1 - 2\sqrt{2}}{2}$
125	$-\cos 120^\circ + \sin 300^\circ + \cos 120^\circ$	$-\frac{\sqrt{3}}{2}$
126	$\sin 135^\circ + \cos 225^\circ - \tan 120^\circ$	$\sqrt{3}$
127	$\cos 150^\circ \sin 90^\circ + 1 - \tan 225^\circ$	$-\frac{\sqrt{3}}{2}$
128	$\sin 330^\circ + 2 \cos 300^\circ + \sin 315^\circ \tan 180^\circ$	$\frac{1}{2}$
129	$4 \left( \sin 150^\circ - \frac{1}{2} \right) + \tan 120^\circ \sin 270^\circ$	$\sqrt{3}$
130	$\cos(-30^\circ) \tan(-45^\circ) - \sin 240^\circ$	0
131	$\sin(330^\circ) \cdot \tan(315^\circ) + \cos(45^\circ) \cdot \cos(135^\circ)$	0
132	$2 \sin(150^\circ) \cdot \sin(30^\circ) + 4 \cos(210^\circ) \cdot \sin(135^\circ)$	$\frac{1}{2} - \sqrt{6}$

133	$\tan 240^\circ(\sin 210^\circ - \sin 30^\circ) + \tan 135^\circ(\sin 240^\circ - \sin 60^\circ)$	0
134	$\sin \frac{11}{6}\pi + \cos \frac{\pi}{3} + 5 \tan \frac{7}{4}\pi$	-5
135	$\sin \frac{\pi}{2} \cos \frac{5}{6}\pi + \frac{\sqrt{3}}{2} + 3 \tan \frac{7}{6}\pi$	$\sqrt{3}$
136	$\sin \frac{5}{4}\pi \sin \frac{\pi}{4} + \sin \frac{2}{3}\pi \cos \frac{\pi}{6}$	$\frac{1}{4}$
137	$4 \cos \frac{3}{4}\pi \sin \frac{5}{3}\pi - 6 \sin \frac{7}{4}\pi \tan\left(-\frac{\pi}{6}\right)$	0
138	$4 \sin \frac{11}{6}\pi - \sqrt{3} \sin \frac{2}{3}\pi + \tan \frac{5}{4}\pi$	$-\frac{5}{2}$
139	$\sin \frac{11}{6}\pi \cdot \cos \frac{2}{3}\pi + \cos \frac{7}{6}\pi \cdot \sin\left(-\frac{\pi}{3}\right) - \left(\sin \frac{5}{6}\pi\right)^2$	$\frac{3}{4}$
140	$\sin \frac{4}{3}\pi \cdot \cos \frac{5}{6}\pi + \sin \frac{11}{6}\pi \cdot \cos \frac{2}{3}\pi - \left[\tan\left(-\frac{\pi}{3}\right)\right]^2$	-2
141	$(1 - \cos(-45^\circ) + \sin(-30^\circ)) \tan^2(-60^\circ)$	$\frac{3(1 - \sqrt{2})}{2}$
142	$\frac{\sin(-90^\circ) + \sec(-45^\circ)}{\cos(-60^\circ)}$	$2(\sqrt{2} - 1)$
143	$\csc(-30^\circ)(\cos^2(-90^\circ) + \cos(-45^\circ)) + 1$	$1 - \sqrt{2}$

144	$2 \sin(-60^\circ) \cos(-30^\circ) + \tan(-45^\circ)$	$-\frac{5}{2}$
145	$\cot(-45^\circ) + \frac{1}{\cos(-270^\circ) + \csc(-30^\circ)}$	$-\frac{3}{2}$
146	$\tan\left(-\frac{\pi}{3}\right)\left(\cot\frac{\pi}{4} + \cot\left(-\frac{\pi}{6}\right)\right)$	$\sqrt{3}(\sqrt{3} - 1)$
147	$\sec(-\pi) + \tan\frac{\pi}{3} + \frac{1}{\csc\frac{\pi}{2}}$	$\sqrt{3}$
148	$\left(1 - \sin\left(-\frac{\pi}{2}\right)\right)\left(1 + \cos\frac{\pi}{3}\right) - 1$	2
149	$2\left(\tan\left(-\frac{\pi}{6}\right) - \sin\left(-\frac{\pi}{4}\right)\right)\left(\cos\pi + \cot\left(-\frac{\pi}{6}\right) + 1\right)$	$2 - \sqrt{6}$
150	$\frac{1 + \cos\left(-\frac{\pi}{3}\right)}{1 - \cos\left(-\frac{\pi}{3}\right)} + \frac{1}{\sec\left(-\frac{\pi}{3}\right)}$	$\frac{7}{2}$
letterali		
151	$\cos(90^\circ - \alpha) + 2 \sin(360^\circ - \alpha) + \sin(180^\circ - \alpha)$	0
152	$\tan(180^\circ + \alpha) \sin(90^\circ - \alpha) + 2 \sin(180^\circ - \alpha)$	$3 \sin \alpha$
153	$\cos \alpha \cos(360^\circ - \alpha) - \cos(90^\circ - \alpha) \sin(360^\circ - \alpha)$	1

154	$\cos(270^\circ - \alpha) + \tan(360^\circ - \alpha) \cos(180^\circ - \alpha)$	0
155	$\cos(360^\circ - \alpha) \sin(90^\circ + \alpha) + [\sin(180^\circ - \alpha)]^2$	1
156	$\frac{1 + \sin(180^\circ - \alpha) \cos(180^\circ - \alpha)}{\sin \alpha} + \frac{1}{\csc \alpha}$	$\frac{2 \sin^2 \alpha - \sin \alpha \cos \alpha + \cos^2 \alpha}{\sin \alpha}$
157	$\left(\frac{1}{\tan(180^\circ - \alpha)} - \csc \alpha\right) \cos(180^\circ - \alpha)$	$(\cos \alpha - 1) \frac{\cos \alpha}{\sin \alpha}$
158	$\sec(180^\circ - \alpha) \cos(180^\circ - \alpha) + \sin \alpha \csc(180^\circ - \alpha)$	2
159	$\frac{\tan^2 \alpha}{\sin^2(180^\circ - \alpha)} + \frac{\sec \alpha}{\csc(180^\circ - \alpha)}$	$\frac{1 + \sin \alpha \cos \alpha}{\cos^2 \alpha}$
160	$\cot(180^\circ - \alpha)(1 - \sec^2 \alpha) + \tan(180^\circ - \alpha)(1 + \csc^2 \alpha)$	$\frac{-1}{\sin \alpha \cos \alpha}$
161	$2 \tan(\pi - \alpha) \cos^2(\pi - \alpha) + \sin \alpha \csc(\pi - \alpha)$	$1 - 2 \sin \alpha \cos \alpha$
162	$\frac{1 - \cos(\pi - \alpha)}{\sin^2(\pi - \alpha)} \tan^2(\pi - \alpha) - 2 \sec^2(\pi - \alpha)$	$\frac{\cos \alpha - 1}{\cos^2 \alpha}$
163	$\left(\frac{1}{1 + \tan(\pi - \alpha)} - \frac{1}{\cot^2(\pi - \alpha)}\right) \cos(\pi - \alpha)$	$\frac{\cos \alpha - 2 \cos^3 \alpha - \sin^3 \alpha}{\cos \alpha (\cos \alpha - \sin \alpha)}$
164	$\sec(\pi - \alpha)(3 - \cos(\pi - \alpha)) + \cot^2(\pi - \alpha)$	$\frac{2 \cos^3 \alpha + 3 \cos^2 \alpha - \cos \alpha - 3}{\cos \alpha - \cos^3 \alpha}$
165	$\frac{\csc(\pi - \alpha) - \cot(-\alpha)}{\cos(\pi - \alpha) \csc \alpha}$	$-\frac{1 + \cos \alpha}{\cos \alpha}$

166	$\frac{1 + \sin(180^\circ + \alpha) \cos(180^\circ + \alpha)}{\sin(180^\circ + \alpha)} - \frac{1}{\sec(180^\circ + \alpha)}$	$-\csc \alpha$
167	$\sec(180^\circ + \alpha) \csc(180^\circ + \alpha)(\tan(180^\circ + \alpha) + \cot \alpha)$	$\sec^2 \alpha \csc^2 \alpha$
168	$\frac{1 + \cos(180^\circ + \alpha)}{1 - \cos(180^\circ + \alpha)} - \frac{1 + 2 \cos(180^\circ + \alpha)}{\sin^2(180^\circ + \alpha)}$	$\cot^2 \alpha$
169	$\tan \alpha(1 + \cot(180^\circ + \alpha)) - 1$	$\tan \alpha$
170	$\sin(180^\circ + \alpha) \cos(180^\circ + \alpha)(\tan \alpha + \cot(180^\circ + \alpha))$	1
171	$\frac{\sin^2(\pi + \alpha) - \sin(\pi + \alpha)}{\cos(\pi + \alpha)} + \frac{1}{\cot \alpha}$	$-\sin \alpha \tan \alpha$
172	$\frac{\cos^2 \alpha - \cos^4(\pi + \alpha)}{1 - \sin^2(\pi + \alpha)} - \sin^2(\pi + \alpha)$	0
173	$\frac{\cot(\pi + \alpha)}{\cot^2(\pi + \alpha) + 1} + \cos \alpha(\tan^2(\pi + \alpha) + 1)$	$\sin \alpha \cos \alpha + \sec \alpha$
174	$\sin(\pi + \alpha) \cos(\pi + \alpha) \csc(\pi + \alpha) - \frac{1 - \sin^2(\pi + \alpha)}{\cos \alpha}$	$-2 \cos \alpha$
175	$\frac{1 - \sin(\pi + \alpha) - \sin^2 \alpha}{\sin(\pi + \alpha) \cos(\pi + \alpha)} + \frac{\cos(\pi + \alpha)}{1 - \sin^2(\pi + \alpha)}$	$\cot \alpha$
176	$\frac{1 + \sec^2(360^\circ - \alpha) (\sin^2(360^\circ - \alpha) + 1)}{2 \sin \alpha \sec^2(360^\circ - \alpha)}$	$\cosec \alpha$
177	$\frac{\sin(360^\circ - \alpha) \cos(360^\circ - \alpha)}{1 - \sin^2 \alpha} + \frac{1}{\cot(360^\circ - \alpha)}$	$-2 \tan \alpha$

178	$\frac{\tan^2(360^\circ - \alpha)}{1 - \tan^2(360^\circ - \alpha)} - \cot(360^\circ - \alpha)$	$\frac{\cot \alpha + \tan^2 \alpha - \tan \alpha}{1 - \tan^2 \alpha}$
179	$\cos^2(360^\circ - \alpha) + \frac{1}{\cot^2(360^\circ - \alpha) + 1}$	1
180	$\frac{1}{\csc^2(360^\circ - \alpha)} + \cos(360^\circ - \alpha) \left( \sin(360^\circ - \alpha) + \frac{1}{\sec \alpha} \right)$	$1 - \sin \alpha \cos \alpha$
181	$\frac{1}{\cos(2\pi - \alpha)(1 + \tan^2(2\pi - \alpha))} + \sec(2\pi - \alpha)$	$(2 + \tan^2 \alpha) \cos \alpha$
182	$-\sin(2\pi - \alpha) \tan \alpha + \frac{1}{\csc(2\pi - \alpha)}$	$\sin \alpha (\tan \alpha - 1)$
183	$\frac{\sin^2(2\pi - \alpha)}{1 - \sin^2 \alpha} - \frac{1 - \cos^2(2\pi - \alpha)}{\cos^2 \alpha}$	0
184	$\csc(2\pi - \alpha)(\cos^2 \alpha - 2\cos^2(2\pi - \alpha) + 1)$	$-\sin \alpha$
185	$\sin(2\pi - \alpha)(\cos^2(2\pi - \alpha) - 1) \frac{1}{\tan^3(2\pi - \alpha)}$	$-\cos^3 \alpha$

4. espressioni di riepilogo con angoli notevoli, angoli superiori a  $360^\circ$  e angoli associati

186	$-2 \sin 90^\circ - 5 \sin 180^\circ + 3 \cos 180^\circ$	-5
187	$4 \sin 135^\circ \cos 0^\circ - 2 \tan 60^\circ - \sqrt{3} \tan 135^\circ$	$2\sqrt{2} - \sqrt{3}$
188	$\sin 60^\circ \sin 120^\circ + \tan 420^\circ \sin 630^\circ$	$\frac{3}{4} - \sqrt{3}$
189	$\sin 270^\circ \tan 30^\circ + 5 \sin 270^\circ \tan 0^\circ + \frac{1}{2} \sin 30^\circ + 2 \cos 180^\circ$	$-\frac{\sqrt{3}}{3} - \frac{7}{4}$

190	$5\sin 90^\circ + 2 \sin 270^\circ - 3 \tan 180^\circ$	3
191	$\cos 270^\circ \tan 30^\circ - 4 \sin 90^\circ \tan 360^\circ + \frac{1}{4} \sin 30^\circ - \frac{1}{2} \cos 180^\circ$	$\frac{5}{8}$
192	$\sin 45^\circ \cos 0^\circ - 3 \tan 30^\circ + \sqrt{3} \tan 45^\circ$	$\frac{\sqrt{2}}{2}$
193	$\cos 30^\circ \sin 150^\circ - \tan 225^\circ \sin 630^\circ$	$\frac{\sqrt{3}}{4} + 1$
194	$\cos 540^\circ + 4 \sin 45^\circ \tan 405^\circ$	$2\sqrt{2} - 1$
195	$(\cos 540^\circ \cos 90^\circ - 1) \sin 630^\circ$	1
196	$4 \cos \frac{9}{2}\pi - \sqrt{3} \cos 5\pi - 2 \cos \frac{13}{6}\pi$	0
197	$\cos \pi - \frac{3}{4} \sin \frac{\pi}{6} + \frac{1}{4} \cos \frac{3}{2}\pi \tan \frac{\pi}{4}$	$-\frac{11}{8}$
198	$3 \left( \tan 30^\circ - \frac{1}{3} \tan 60^\circ \right) + 4 \sin 45^\circ \cos 45^\circ$	4
199	$4 \tan \frac{\pi}{4} - \sin \frac{3}{2}\pi + 4 \left( \sin \frac{\pi}{6} - 2 \sin \frac{\pi}{4} \right) + \left( \tan \frac{\pi}{3} \right)^2 - 10$	$-4\sqrt{2}$
200	$\left( 7 \cos 0 - 2 \sin \pi - 5 \sin \frac{3}{2}\pi \cos \pi \right)^2 - 4 \sin \pi$	4
201	$4 \sin \frac{9}{4}\pi - \left( 2 \cos \frac{\pi}{4} \right)^2 + \cos \frac{5}{2}\pi$	$2\sqrt{2} - 2$

202	$\sqrt{3}\sin(-30^\circ) - 2\cos 240^\circ \sin 120^\circ - \frac{1}{3}\tan 300^\circ$	$\frac{\sqrt{3}}{3}$
203	$\cos \frac{\pi}{6} \tan\left(-\frac{\pi}{4}\right) + 2\left(\sin \frac{3}{4}\pi\right)^2 + \cos \frac{\pi}{2} \sin \frac{9}{4}\pi$	$-\frac{\sqrt{3}}{2} + 1$
204	$\sqrt{6} \sin \frac{3}{2}\pi + \cos\left(-\frac{\pi}{6}\right) \cos \frac{5}{4}\pi + \sqrt{2} \tan \frac{2}{3}\pi$	$\frac{9}{4}\sqrt{6}$
205	$\sin^2(180^\circ - \alpha) - 1 + \cos(360^\circ - \alpha) + \cos^2(-\alpha)$	$\cos \alpha$
206	$2\sin^2(180^\circ + \alpha) + \cos^4(180^\circ - \alpha) \tan^2(180^\circ + \alpha) - \sin^4(180^\circ - \alpha)$	$\sin^2 \alpha (3 - 2 \sin^2 \alpha)$
207	$\frac{a \cos(-45^\circ) - \tan(-30^\circ)}{-\frac{3}{2}b \csc(-30^\circ)}$	$\frac{3a\sqrt{2} + 2\sqrt{3}}{18b}$
208	$\sec(360^\circ - \alpha)(\sin(360^\circ - \alpha) \cos(360^\circ - \alpha) - 1) + \frac{\tan \alpha}{\sin(180^\circ - \alpha)}$	$-\sin \alpha$
209	$\frac{1 - \cos^2(360^\circ - \alpha)}{\sin(180^\circ + \alpha) \cos(360^\circ - \alpha)} + \frac{1}{\sin \alpha \cos(180^\circ + \alpha)}$	$-\frac{\sin^2 \alpha + 1}{\sin \alpha \cos \alpha}$
210	$\left(\frac{\cot^2(-30^\circ)}{a \sin(-30^\circ)} \frac{b^2 \cos(-30^\circ)}{\tan(-30^\circ)}\right)^{\frac{1}{2}}$	$\frac{3b}{\sqrt{a}}$
211	$\csc(360^\circ - \alpha) - \cos(180^\circ + \alpha) \cot(180^\circ - \alpha)$	$\frac{\sin^2 \alpha - 2}{\sin \alpha}$

212	$\cos^2(\pi - \alpha) \tan \alpha - \cos^2(-\alpha) \cot(\pi - \alpha)$	$\cot \alpha$
213	$\frac{\sqrt{a}}{2} \cot^2(-45^\circ) + \frac{\sqrt{b}}{a} \frac{\sin(-45^\circ)}{1 + \cos(-60^\circ)}$	$\frac{\sqrt{a}}{2} - \frac{\sqrt{2b}}{3a}$
214	$a \cos^2(-30^\circ) (4b^2 \cos(-45^\circ) + 1)$	$\frac{3}{4}a(1 + 2\sqrt{2}b^2)$
215	$\cos \alpha - \frac{\cos^2(\pi + \alpha) - \sin^2(2\pi - \alpha)}{\sin(2\pi - \alpha) - \cos(2\pi - \alpha)}$	$2 \cos \alpha - \sin \alpha$
216	$\frac{3b \left( \tan\left(-\frac{\pi}{3}\right) - \cot\left(-\frac{\pi}{3}\right) \right)}{2a \left( \tan\left(-\frac{\pi}{6}\right) + \cot\frac{\pi}{6} \right)}$	$-\frac{3b}{2a}$
217	$\sin(\pi + \alpha) \csc(2\pi - \alpha) (\tan(-\alpha) + \cot \alpha)$	$\frac{1 - 2 \sin^2 \alpha}{\sin \alpha \cos \alpha}$
218	$\frac{(b+c) \sec(-45^\circ) + (b-c) \csc(-45^\circ)}{\tan(-60^\circ) \cot(-30^\circ)}$	$\frac{2\sqrt{2}c}{3}$
219	$\cos(2\pi + \alpha) \tan(\pi - \alpha) + \sin(\pi - \alpha) \cot(2\pi + \alpha)$	$\cos \alpha - \sin \alpha$
220	$b^3 \cos\left(-\frac{\pi}{4}\right) \left(1 + \tan^2\left(\frac{\pi}{4}\right)\right) + \sqrt[3]{b} \cot^2\left(-\frac{\pi}{3}\right)$	$\sqrt{2}b^3 + \frac{1}{3}\sqrt[3]{b}$

221	$\frac{2a + \sin\left(-\frac{\pi}{3}\right)}{\cos^2\left(-\frac{\pi}{3}\right)} + \frac{3b - \cos\left(-\frac{\pi}{6}\right)}{\sin^2\left(-\frac{\pi}{6}\right)}$	$4(2a - \sqrt{3} + 3b)$
222	$csc(\pi - \alpha)(1 - \sin^2(\pi + \alpha))$	$\cot \alpha \cos \alpha$
223	$\frac{3}{2}\sqrt{a} \tan^2\left(-\frac{\pi}{4}\right) \frac{\sec\left(-\frac{\pi}{4}\right)}{\csc\left(-\frac{\pi}{4}\right)} \frac{\sqrt{a}}{a}$	$-\frac{3}{2}$
224	$\left(2a \sin\left(-\frac{\pi}{3}\right) - 2b \cos\left(-\frac{\pi}{3}\right)\right)^2 + \frac{\sqrt{b}}{b}$	$(a\sqrt{3} + b)^2 + \frac{\sqrt{b}}{b}$
<b>esercizi più impegnativi</b>		
225	$\sin^2 15^\circ$	$\frac{2 - \sqrt{3}}{4}$
226	$\cos 75^\circ \cos 15^\circ$	$\frac{1}{4}$
227	$\frac{\tan^2 22,5^\circ}{4} + \sin 45^\circ$	$\frac{3}{4}$
228	$\frac{\cos 72^\circ}{\sin^2 30^\circ} + \tan 45^\circ$	$\sqrt{5}$
229	$\tan 7,5^\circ \tan 67,5^\circ - 3 \tan 30^\circ$	$-\sqrt{2}$
230	$\tan 15^\circ + \frac{\tan 21^\circ + \tan 39^\circ}{1 - \tan 21^\circ \tan 39^\circ}$	2
231	$\sin 18^\circ \tan 9^\circ$	$1 - \frac{\sqrt{10 + 2\sqrt{5}}}{4}$

232	$\frac{\sin 72^\circ \sin 36^\circ}{\sin 18^\circ} + \tan^2 72^\circ$	$\frac{25 + 9\sqrt{5}}{4}$
233	$(\sin 18^\circ \tan 9^\circ)^2 + 2 \cos 18^\circ$	$\frac{13 + \sqrt{5}}{8}$
234	$(\sin 162^\circ + \sin 126^\circ) \csc 60^\circ$	$\frac{\sqrt{15}}{3}$
235	$\cos^2 54^\circ \sec^2 36^\circ$	$5 - 2\sqrt{5}$
236	$(2 \sin^2 67,5^\circ - \cos 45^\circ) \cot 22,5^\circ$	$1 + \sqrt{2}$
237	$\tan 37,5^\circ + \sqrt{2} \tan 67,5^\circ$	$\sqrt{3} + \sqrt{6}$
238	$\cos 85^\circ \cos 13^\circ + \sin 85^\circ \sin 13^\circ$	$\frac{\sqrt{5} - 1}{4}$
239	$\frac{1}{2}(\sqrt{3} \cos 6^\circ - \sin 6^\circ)$	$\frac{\sqrt{5} + 1}{4}$
240	$\frac{\sqrt{3} - \tan 24^\circ}{1 + \sqrt{3} \tan 24^\circ}$	$\sqrt{5 - 2\sqrt{5}}$
241	$\frac{(\tan 22^\circ - \tan 5^\circ) \cot 17^\circ \cot 5^\circ}{\cot 5^\circ + \tan 22^\circ}$	1
242	$16 \sin^5 18^\circ - 20 \sin^3 18^\circ + 5 \sin 18^\circ$	1
243	$\cos 9^\circ - \sin 9^\circ$	$\frac{\sqrt{5 - \sqrt{5}}}{2}$

244	$8 \cos^3 20^\circ - 6 \cos 20^\circ$	1
5. espressioni risolubili con le formule di addizione e sottrazione <span style="color: red;">↑</span>		
245	$\sin(\alpha + \beta) \sin(\alpha - \beta)$	$\sin^2 \alpha - \sin^2 \beta$
246	$\cos(\alpha + \beta) \cos(\alpha - \beta)$	$\cos^2 \alpha - \sin^2 \beta$
247	$\cos(\alpha - \beta) \cos \alpha + \sin(\alpha - \beta) \sin \alpha$	$\cos \beta$
248	$\frac{\cos(\alpha + \beta) + \cos(\alpha - \beta)}{\sin(\alpha + \beta) + \sin(\alpha - \beta)}$	$\cot \alpha$
249	$\frac{\cos(\alpha - \beta)}{\sin \beta \cos \alpha}$	$\tan \alpha + \cot \beta$
250	$\tan(\alpha + \beta) \tan(\alpha - \beta)$	$\frac{\tan^2 \alpha - \tan^2 \beta}{1 - \tan^2 \alpha \tan^2 \beta}$
251	$\frac{\tan(\alpha + \beta)}{\cot(\alpha - \beta)}$	$\frac{\tan \alpha \cot \beta - \tan \beta \cot \alpha}{\cot \alpha \cot \beta - \tan \alpha \tan \beta}$
6. espressioni risolubili con le formule di duplicazione e bisezione <span style="color: red;">↑</span>		
252	$\sin^2 2\alpha + \cos 2\alpha + 4 \sin^4 \alpha$	$2 \sin^2 \alpha + 1$
253	$(1 + \cos 2\alpha) \tan \alpha$	$\sin 2\alpha$
254	$\sin 2\alpha (\tan \alpha + \cot \alpha)$	2

255	$\frac{1 - \cos 2\alpha}{2} (\cot^2 \alpha - 1)$	$\cos 2\alpha$
256	$\frac{1}{2} \tan 2\alpha (1 + \tan \alpha)$	$\frac{\tan \alpha}{1 - \tan \alpha}$
257	$2 \tan^2 \alpha \sin^2 \frac{\alpha}{2} + \tan \alpha \sin \alpha$	$\tan^2 \alpha$
258	$\frac{1 - \cos \alpha}{2} \left( \cot^2 \frac{\alpha}{2} - 1 \right)$	$\cos \alpha$
259	$\frac{1}{1 - \tan^2 \frac{\alpha}{2}} - \frac{1}{1 - \cot^2 \frac{\alpha}{2}}$	$\frac{1}{\cos \alpha}$

## 7. espressioni risolubili con le formule di prostaferesi e Werner



260	$\cos(60^\circ + \alpha) + \cos(60^\circ - \alpha)$	$\cos \alpha$
261	$\cot(45^\circ + \alpha) + \cot(45^\circ - \alpha)$	$\frac{2}{\cos 2\alpha}$
262	$\tan 7\alpha + \tan 3\alpha$	$\frac{\sin 10\alpha}{\cos 7\alpha \cos 3\alpha}$
263	$\sin \alpha \sin \beta - \frac{1}{2} \cos(\alpha - \beta)$	$-\frac{1}{2} \cos(\alpha + \beta)$
264	$\frac{\sin \alpha - \sin \beta}{\cos \alpha + \cos \beta}$	$\tan \frac{\alpha - \beta}{2}$
265	$\sin\left(\frac{\pi}{3} + \alpha\right) + \sin\left(\frac{\pi}{3} - \alpha\right)$	$\sqrt{3} \cos \alpha$

266	$\tan\left(\frac{\pi}{4} + \alpha\right) - \tan\left(\frac{\pi}{4} - \alpha\right)$	$2 \tan 2\alpha$
267	$\frac{\sin\left(\frac{\pi}{3} + \alpha\right) + \cos\left(\frac{5}{6}\pi - \alpha\right)}{\cos\left(\frac{\pi}{3} + \alpha\right) + \sin\left(\frac{5}{6}\pi - \alpha\right)}$	$\tan \alpha$
268	$2 \sin \alpha \cos 3\alpha$	$\sin 4\alpha - \sin 2\alpha$
269	$\frac{\cos\left(\alpha - \frac{\pi}{4}\right) \sin\left(\frac{3}{4}\pi + \alpha\right)}{\cos \alpha + \sin \alpha}$	$\frac{1}{2}(\cos \alpha - \sin \alpha)$

## 8. espressioni di riepilogo con le formule goniometriche



270	$\frac{1}{2} \sin 2(\alpha + \beta)$	$\sin \alpha \cos \alpha \cos 2\beta + \sin \beta \cos \beta \cos 2\alpha$
271	$\cos^4 \alpha - \sin^4 \alpha$	$\cos 2\alpha$
272	$\cos^4 \frac{\alpha}{2} - \sin^4 \frac{\alpha}{2}$	$\cos \alpha$
273	$\frac{\cos 8\alpha + \cos \alpha}{\cos 8\alpha - \cos \alpha}$	$-\cot \frac{9}{2}\alpha \cot \frac{7}{2}\alpha$
274	$\frac{\sin(3\alpha + \beta) \sin(3\alpha - \beta) - \sin(\alpha + \beta) \sin(\alpha - \beta)}{\sin 4\alpha \sin 2\alpha}$	1
275	$2 \tan \alpha \sin^2 \frac{\alpha}{2} + \sin \alpha$	$\tan \alpha$
276	$\sin \alpha \cos(\alpha + \beta) - \cos \alpha \sin(\alpha + \beta)$	$\cos\left(\frac{\pi}{2} + \beta\right)$

277	$\frac{\sin^2 \alpha - \sin^2 \beta}{\cos^2 \alpha - \cos^2 \beta}$	-1
278	$\frac{2 \sin 3\alpha \sin 8\alpha}{\sin 5\alpha + \sin 8\alpha}$	$\frac{\cos 5\alpha - \cos 11\alpha}{2 \sin \frac{13}{2}\alpha \cos \frac{3}{2}\alpha}$
279	$\frac{2\tan\left(\frac{\pi}{2} - \alpha\right)}{1 + [\cot(\pi - \alpha)]^2} - [\cos\left(\frac{\pi}{2} - \alpha\right) + \sin\left(\frac{\pi}{2} - \alpha\right)]$	$\sin 2\alpha - \sin \alpha - \cos \alpha$

## 9. espressioni con funzioni goniometriche inverse



280	$\tan\left(\arccos\left(-\frac{\sqrt{2}}{2}\right)\right)$	-1
281	$\tan\left(\arcsin\frac{\sqrt{3}}{2}\right)$	$\sqrt{3}$
282	$\frac{3}{4} + \cot\left(\arcsin\frac{\sqrt{2}}{2}\right) - \frac{1}{2} \cos(\operatorname{arccot} 0)$	$\frac{7}{4}$
283	$\sqrt{2}\sin\left(\arccos\frac{\sqrt{2}}{2}\right) - \frac{1}{2} + \frac{3}{2}\tan(\operatorname{arccot}\sqrt{3})$	$\frac{1 + \sqrt{3}}{2}$
284	$\sin(\operatorname{arctan} 1)$	$\frac{\sqrt{2}}{2}$
285	$\csc\left(\operatorname{arctan}\left(-\frac{\sqrt{3}}{3}\right)\right)$	-2
286	$\cos\left(\operatorname{arccot}(-\sqrt{3})\right)$	$-\frac{\sqrt{3}}{2}$

287	$\sin(\arccos 1)$	0
288	$\sin(\arctan \sqrt{3})$	$\frac{\sqrt{3}}{2}$

## 10. espressioni da ricondurre ad altre equivalenti prive di funzioni goniometriche inverse



289	$\cos(\arccos x)$	$x, x \in [-1, 1]$
290	$\arccos(\cos x) \quad x \in [-\pi, \pi]$	$ x $
291	$\cos(\arcsin x)$	$\sqrt{1 - x^2}$
292	$\cos(\arcsin x - \arccos x)$	$2x\sqrt{1 - x^2}$
293	$\sin(3 \arcsin x)$	$x(3 - 4x^2), x \in [-1, 1]$
294	$\tan(\arcsin x) + \tan(\arccos x)$	$\frac{1}{x\sqrt{1 - x^2}}$
295	$\tan(\arcsin x + \arccos x)$	impossibile
296	$\sin(2 \arccos x - 2 \arcsin x)$	$4x(1 - 2x^2)\sqrt{1 - x^2}$
297	$\frac{\cos(\arcsin x)}{\sin(\arccos x)}$	$1, x \in [-1, 1]$

298	$\tan \frac{\pi}{4} - \sin\left(\arcsin x + \frac{\pi}{2}\right) \cos\left(\arccos x - \frac{\pi}{2}\right)$	$x^2, \quad x \in [-1, 1]$
299	$\frac{\cos(\arcsin x^2) - \cos^2(\arcsin x)}{\sin(\arccos x)}$	$\sqrt{1+x^2} - \sqrt{1-x^2} \wedge x \neq \pm 1$
300	$\sin(\arctan \sqrt{x}) + \sin\left(\arctan \frac{1}{\sqrt{x}}\right)$	$\frac{\sqrt{x}+1}{\sqrt{x}+1}$
301	$\sin(\arcsin x + \arccos x^2 + \arctan x)$	$1 - \frac{x^2(\sqrt{1-x^2}+1)(\sqrt{1+x^2}-x)}{\sqrt{1+x^2}}$
302	$2 \sin(\arccos(\sin x)) \cos(\arcsin(\cos x))$	$ \sin 2x $
303	$\sin(\arccos(\sin(\arccos x))) - \sin(\arcsin(\cos(\arccos x)))$	$ x  - x, \quad x \in [-1, 1]$
304	$\frac{\sin^2(\arctan \sqrt{x})}{\sin^2(\arccos \sqrt{x})} - x$	$\frac{x^3}{1-x^2}, \quad x \in [0,1)$
305	$\cos^2\left(\arctan \frac{1}{\sqrt{x}}\right) \sin^2\left(\arctan \frac{1}{\sqrt{x}}\right)$	$\frac{x}{(x+1)^2}$
306	$1 + \tan^2(\arcsin(1-\sqrt{x}))$	$\frac{1}{2\sqrt{x}-x}, \quad x \in (0,4)$
307	$\cos\left(\arctan x + \arctan \frac{1}{x}\right) + \sin\left(\arctan x + \arctan \frac{1}{x}\right)$	$\frac{x}{ x }$
308	$\sqrt{\sin\left(3 \arctan \sqrt{x} + 3 \arctan \frac{1}{\sqrt{x}}\right)}$	impossibile