

Espressioni goniometriche

di angoli notevoli

1	$\left(\sin 360^\circ + \frac{1}{2}\cos 180^\circ\right) \operatorname{ctg} 90^\circ$	0
2	$\left(\operatorname{tg} 0^\circ - \frac{1}{3}\sin 270^\circ\right)^{\frac{1}{2}}$	$\frac{\sqrt{3}}{3}$
3	$(\sec 180^\circ + \operatorname{cosec} 90^\circ)(1 + \cos 0^\circ)$	0
4	$\frac{\cos 270^\circ + \operatorname{tg} 180^\circ}{3 \operatorname{cosec} 90^\circ}$	0
5	$\sin^2 90^\circ + \cos^2 360^\circ$	2
6	$\left(\operatorname{tg} \pi + \operatorname{ctg} \frac{\pi}{2}\right) \cos 0$	0
7	$\frac{\cos \pi + \frac{1}{2}\cos \frac{\pi}{2}}{2 \sin \frac{3}{2}\pi}$	$\frac{1}{2}$
8	$\sec \pi (\sin^2 2\pi + \cos 0)$	-1
9	$\sec 0 \sin \pi + \sqrt{5} \sin \frac{\pi}{2}$	$\sqrt{5}$
10	$\frac{1 + \operatorname{tg} \pi}{\operatorname{cosec} \frac{\pi}{2}}$	1
11	$(4 \sin 30^\circ + \sqrt{2} \operatorname{tg} 45^\circ) \left(1 + \frac{1}{3} \cos 30^\circ\right)$	$(2 + \sqrt{2}) \left(1 + \frac{\sqrt{3}}{6}\right)$
12	$4 \cos 45^\circ \sin^2 60^\circ$	$\frac{3}{2}\sqrt{2}$
13	$(\sin 60^\circ + \operatorname{ctg}^2 45^\circ) \frac{1}{\sin 30^\circ}$	$\sqrt{3} + 2$
14	$1 - \sin 45^\circ \cos 45^\circ$	$\frac{1}{2}$
15	$\operatorname{tg}^2 30^\circ \sin^2 60^\circ$	$\frac{1}{4}$
16	$\left(\sin \frac{\pi}{3} + \cos \frac{\pi}{6}\right) \frac{1}{\operatorname{tg} \frac{\pi}{3}}$	1

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17	$\left(\sqrt{3} \cos \frac{\pi}{6} + \sin \frac{\pi}{6}\right) \operatorname{ctg}^2 \frac{\pi}{4}$	2
18	$\sqrt{2} \cos \frac{\pi}{4} + 2\sqrt{3} \sin \frac{\pi}{3}$	4
19	$\operatorname{cosec} \frac{\pi}{4} \frac{1}{\sec \frac{\pi}{3}}$	$\frac{\sqrt{2}}{2}$
20	$\frac{3 \operatorname{tg} \frac{\pi}{6} + \operatorname{tg} \frac{\pi}{3}}{\operatorname{tg} \frac{\pi}{4}}$	$2\sqrt{3}$
21	$\frac{a \operatorname{cosec}^2 90^\circ + b \sec^2 0^\circ}{a \sin 270^\circ}$	$-\frac{a+b}{a}$
22	$(2a \cos 180^\circ)^2 + (2b \cos 270^\circ)^2$	$4a^2$
23	$\left(\frac{\sqrt{a} \sec 0^\circ}{a \cos 180^\circ}\right) \sin 270^\circ$	$\frac{\sqrt{a}}{a}$
24	$\frac{b - \cos 90^\circ}{\sin 270^\circ} - \frac{a}{\sec 0^\circ}$	$-(a+b)$
25	$\sqrt[3]{a} \operatorname{tg} 0^\circ - \frac{b}{\operatorname{ctg}^2 90^\circ - 1}$	b
26	$(\operatorname{tg}^2 \pi + a) \cos 0 + \sin \frac{3}{2} \pi$	$a - 1$
27	$\frac{a \cos \pi + \sin \frac{\pi}{2}}{a \operatorname{cosec} \frac{3}{2} \pi + b \sec \pi}$	$\frac{a-1}{a+b}$
28	$\frac{4a\sqrt{3} \sin \frac{3}{2} \pi - b \cos \frac{\pi}{2}}{a \operatorname{cosec} \frac{3}{2} \pi}$	$4\sqrt{3}$
29	$b \cos 2\pi (\sec 0 + a \operatorname{tg} 2\pi)$	b
30	$\sec 2\pi \operatorname{tg}^2 \pi + 3a \sin \frac{3}{2} \pi$	$-3a$
31	$\sqrt{2ab(\sin^2 30^\circ + \operatorname{ctg} 45^\circ)}$	$\frac{\sqrt{10ab}}{2}$
32	$\frac{3}{2} a \operatorname{cosec} 60^\circ (b \cos 45^\circ - c \operatorname{tg} 30^\circ)$	$\frac{\sqrt{6}ab}{2} - ac$

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33	$\sqrt{a} \operatorname{ctg} 45^\circ + \frac{b \operatorname{sen} 45^\circ}{1 + c \operatorname{tg} 30^\circ}$	$\sqrt{a} + \frac{3}{2} \sqrt{2} \frac{b}{3 + \sqrt{3}c}$
34	$\frac{b^2 \operatorname{cosec}^2 60^\circ}{\operatorname{sen} 30^\circ} + \frac{a}{\operatorname{sec}^2 60^\circ}$	$\frac{8}{3} b^2 + \frac{a}{4}$
35	$\frac{2a + \operatorname{sen} 45^\circ}{b \cos 60^\circ} \operatorname{ctg} 30^\circ$	$\frac{2\sqrt{3}}{b} \left(2a + \frac{\sqrt{2}}{2} \right)$
36	$\frac{\sqrt{a} \operatorname{sen} \frac{\pi}{3} \sqrt{b} \operatorname{tg} \frac{\pi}{4}}{c \operatorname{cosec} \frac{\pi}{6}}$	$\frac{\sqrt{3ab}}{c}$
37	$\left(a \operatorname{tg} \frac{\pi}{3} - b \operatorname{ctg} \frac{\pi}{6} \right) b \operatorname{cosec}^2 \frac{\pi}{4}$	$2\sqrt{3}b(a - b)$
38	$\left(1 - a \operatorname{sen} \frac{\pi}{4} - b \operatorname{sen} \frac{\pi}{6} \operatorname{tg}^2 \frac{\pi}{4} \right)^{\frac{1}{3}}$	$\left(1 - \frac{a\sqrt{2}}{2} - \frac{b}{2} \right)^{\frac{1}{3}}$
39	$\frac{\sqrt{2a} \operatorname{cosec} \frac{\pi}{4}}{1 + b \operatorname{sec} \frac{\pi}{3}} b \operatorname{ctg} \frac{\pi}{4}$	$\frac{2\sqrt{a}b}{1 + 2b}$
40	$\left(a \cos^2 \frac{\pi}{4} + b \operatorname{sen} \frac{\pi}{6} \right) c \operatorname{cosec} \frac{\pi}{3}$	$\left(\frac{a+b}{\sqrt{3}} \right) c$

con angoli superiori a 360°

41	$(\operatorname{cos} 360^\circ + 2 \operatorname{cos} 450^\circ)(1 - \operatorname{tg} 540^\circ)$	1
42	$\sqrt{2} \operatorname{sen} 450^\circ + \operatorname{tg}^2 360^\circ$	$\sqrt{2}$
43	$\left(3 \operatorname{tg} 540^\circ + \frac{2}{5} \operatorname{ctg} 450^\circ \right)^{\frac{\sqrt{2}}{2}}$	0
44	$\operatorname{sen} 630^\circ + \frac{\operatorname{cos}^2 540^\circ}{\operatorname{sen} 450^\circ}$	0
45	$\operatorname{sec} 360^\circ \operatorname{cosec} 450^\circ + \sqrt{3} \operatorname{tg} 540^\circ$	1
46	$\left(\operatorname{cos} \frac{5}{2}\pi + \frac{1}{2} \operatorname{cos} 3\pi \right) \operatorname{sen} \frac{3}{2}\pi$	$\frac{1}{2}$
47	$\frac{\operatorname{tg} \pi + \operatorname{ctg} \frac{\pi}{2}}{\operatorname{cos} 2\pi}$	0
48	$\frac{1}{10} \operatorname{sec} 3\pi \operatorname{cosec} \frac{3}{2}\pi$	$\frac{1}{10}$

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49	$\sqrt{3} \sin \frac{5}{2}\pi \frac{1}{3} \cos 2\pi$	$\frac{\sqrt{3}}{3}$
50	$(1 - \cos \frac{3}{2}\pi)(1 + \cos 2\pi)$	2
51	$2 \sin 390^\circ + \frac{\cos^2 390^\circ}{\sin 405^\circ}$	$\frac{4+3\sqrt{2}}{4}$
52	$\frac{1 - \cos 420^\circ}{1 + \cos 420^\circ} - \operatorname{ctg}^2 390^\circ$	$-\frac{8}{3}$
53	$\operatorname{tg} 405^\circ(1 + \operatorname{ctg} 390^\circ) - 1$	$\sqrt{3}$
54	$\frac{\sec 390^\circ}{1 + \operatorname{tg}^2 420^\circ} + \frac{1}{\operatorname{cosec} 390^\circ}$	$\frac{\sqrt{3}+3}{6}$
55	$\operatorname{ctg}^2 420^\circ - \operatorname{cosec}^2 390^\circ + \frac{1}{\sec 405^\circ}$	$\frac{3\sqrt{2}-22}{6}$
56	$\left(\operatorname{tg} \frac{9}{4}\pi + 1\right) \sec \frac{7}{3}\pi$	4
57	$\left(\frac{\cos \frac{9}{4}\pi}{1 - \sin \frac{13}{6}\pi}\right) - \sin \frac{9}{4}\pi$	$\frac{\sqrt{2}}{2}$
58	$\frac{\operatorname{ctg}^2 \frac{13}{6}\pi - \cos^2 \frac{7}{3}\pi}{\operatorname{cosec} \frac{7}{3}\pi}$	$\frac{11}{8}\sqrt{3}$
59	$\cos \frac{9}{4}\pi + \frac{\sin^2 \frac{9}{4}\pi}{\cos \frac{7}{3}\pi}$	$\frac{2+\sqrt{2}}{2}$
60	$\frac{\operatorname{cosec} \frac{7}{3}\pi}{\operatorname{sec} \frac{7}{3}\pi} \operatorname{tg} \frac{9}{4}\pi$	$\frac{\sqrt{3}}{3}$
61	$a\sqrt{3}(\cos^2 360^\circ + \operatorname{ctg} 450^\circ)$	$\sqrt{3}a$
62	$\frac{\sec 360^\circ}{a} (\sqrt{a} \sin^2 540^\circ - b \cos^2 540^\circ)$	$-\frac{b}{a}$
63	$(\sin 630^\circ + a^2 \cos 630^\circ)^2$	1
64	$\frac{-b \cos 360^\circ - a \sin 630^\circ}{(a+b) \sec 540^\circ}$	$\frac{b-a}{a+b}$

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65	$\sqrt{c} \left(\frac{\sqrt{3}}{2} a \sec 540^\circ + \frac{\sqrt{2}}{3} b \operatorname{cosec} 450^\circ \right)$	$\frac{\sqrt{2c}}{3} b - \frac{\sqrt{3ca}}{2}$
66	$\left(a \cos 3\pi + \sin \frac{5}{2}\pi \right)^2 + \left(\cos \frac{5}{2}\pi - \sqrt{b} \sin \frac{7}{2}\pi \right)^2$	$b + (1-a)^2$
67	$\frac{a^2 \operatorname{cosec} \frac{7}{2}\pi + b \sec 2\pi}{a \cos 3\pi - b^3 \sin 2\pi}$	$\frac{a^2 - b}{a}$
68	$\left(b^4 \tan 2\pi + a^6 \operatorname{cosec} \frac{7}{2}\pi \right)^2 2ab \sin \frac{7}{2}\pi$	$-2a^{13}b$
69	$(1 + a \tan^2 3\pi) \sqrt{b} \sin \frac{5}{2}\pi$	\sqrt{b}
70	$a^2 \cos^4 3\pi - b^3 \sin^4 3\pi - \frac{2c^4}{\sec \frac{7}{2}\pi}$	a^2
71	$\sin^2 390^\circ \frac{\sqrt{ab}}{\operatorname{cosec} 420^\circ} + a \cot 405^\circ$	$\frac{\sqrt{3ab}}{8} + a$
72	$\frac{a \tan 420^\circ}{b - \cot 405^\circ} c \sec^2 390^\circ$	$\frac{4ac\sqrt{3}}{3(b-1)}$
73	$(\sin 420^\circ + a^3 \tan 405^\circ) \cot 405^\circ - 3a^3$	$\frac{\sqrt{3}}{2} - 2a^3$
74	$(\sqrt{a} \tan^2 420^\circ - 1) \sec^2 390^\circ + 1$	$\frac{4}{3}(3\sqrt{a} - 1) + 1$
75	$\left(\frac{(2b \tan 405^\circ)^2}{\cos^2 420^\circ} \right)^{\frac{1}{4}}$	$2\sqrt{b}$
76	$\left(2a \tan^2 \frac{13}{6}\pi - 1 \right) b \cos^2 \frac{9}{4}\pi$	$\frac{b}{6}(2a-3)$
77	$\left(4b \sin \frac{13}{6}\pi + 6a \sin^2 \frac{9}{4}\pi \right) \frac{1}{\operatorname{cosec} \frac{7}{3}\pi(a+b) \cot \frac{13}{6}\pi}$	$\frac{2b+3a}{2(a+b)}$
78	$\left(\frac{a + \sin \frac{9}{4}\pi - b \cos \frac{9}{4}\pi}{1 + \sin^2 \frac{9}{4}\pi + b \cos \frac{9}{4}\pi} \right)^{\frac{1}{2}}$	$\sqrt{\frac{2a + \sqrt{2}(1-b)}{3 + \sqrt{2}b}}$
79	$\frac{\left(b - 3 \cot^2 \frac{7}{3}\pi \right) \left(b \tan \frac{9}{4}\pi + 2 \cos \frac{7}{3}\pi \right)}{2b \operatorname{cosec} \frac{13}{6}\pi - 1}$	$\frac{(b-1)(b+1)}{4b-1}$
80	$\frac{\sqrt{ab} \cos \frac{13}{6}\pi \left(1 + a \sin^2 \frac{9}{4}\pi \right)^2}{\left(2 \cot^2 \frac{9}{4}\pi + \frac{a}{2} \sec \frac{7}{3}\pi \right)^2}$	$\frac{\sqrt{3ab}}{8}$

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con angoli associati

81	$\frac{1 + \sin(180^\circ - \alpha) \cos(180^\circ - \alpha)}{\sin \alpha} + \frac{1}{\cosec \alpha}$	$\frac{2 \sin^2 \alpha - \sin \alpha \cos \alpha + \cos^2 \alpha}{\sin \alpha}$
82	$\left(\frac{1}{\tg(180^\circ - \alpha)} - \cosec \alpha \right) \cos(180^\circ - \alpha)$	$(\cos \alpha - 1) \frac{\cos \alpha}{\sin \alpha}$
83	$\sec(180^\circ - \alpha) \cos(180^\circ - \alpha) + \sin \alpha \cosec(180^\circ - \alpha)$	2
84	$\frac{\tg^2 \alpha}{\sin^2(180^\circ - \alpha)} + \frac{\sec \alpha}{\cosec(180^\circ - \alpha)}$	$\frac{1 + \sin \alpha \cos \alpha}{\cos^2 \alpha}$
85	$\ctg(180^\circ - \alpha)(1 - \sec^2 \alpha) + \tg(180^\circ - \alpha)(1 + \cosec^2 \alpha)$	$\frac{-1}{\sin \alpha \cos \alpha}$
86	$2 \tg(\pi - \alpha) \cos^2(\pi - \alpha) + \sin \alpha \cosec(\pi - \alpha)$	$1 - 2 \sin \alpha \cos \alpha$
87	$\frac{1 - \cos(\pi - \alpha)}{\sin^2(\pi - \alpha)} \tg^2(\pi - \alpha) - 2 \sec^2(\pi - \alpha)$	$\frac{\cos \alpha - 1}{\cos^2 \alpha}$
88	$\left(\frac{1}{1 + \tg(\pi - \alpha)} - \frac{1}{\ctg^2(\pi - \alpha)} \right) \cos(\pi - \alpha)$	$\frac{\cos \alpha - 2 \cos^3 \alpha - \sin^3 \alpha}{\cos \alpha (\cos \alpha - \sin \alpha)}$
89	$\sec(\pi - \alpha)(3 - \cos(\pi - \alpha)) + \ctg^2(\pi - \alpha)$	$\frac{2 \cos^3 \alpha + 3 \cos^2 \alpha - \cos \alpha - 3}{\cos \alpha - \cos^3 \alpha}$
90	$\frac{\cosec(\pi - \alpha) - \ctg(-\alpha)}{\cos(\pi - \alpha) \cosec \alpha}$	$-\frac{1 + \cos \alpha}{\cos \alpha}$
91	$\frac{1 + \sin(180^\circ + \alpha) \cos(180^\circ + \alpha)}{\sin(180^\circ + \alpha)} - \frac{1}{\sec(180^\circ + \alpha)}$	$-\cosec \alpha$
92	$\sec(180^\circ + \alpha) \cosec(180^\circ + \alpha) (\tg(180^\circ + \alpha) + \ctg \alpha)$	$\sec^2 \alpha \cosec^2 \alpha$
93	$\frac{1 + \cos(180^\circ + \alpha)}{1 - \cos(180^\circ + \alpha)} - \frac{1 + 2 \cos(180^\circ + \alpha)}{\sin^2(180^\circ + \alpha)}$	$\ctg^2 \alpha$
94	$\tg \alpha (1 + \ctg(180^\circ + \alpha)) - 1$	$\tg \alpha$
95	$\sin(180^\circ + \alpha) \cos(180^\circ + \alpha) (\tg \alpha + \ctg(180^\circ + \alpha))$	1
96	$\frac{\sin^2(\pi + \alpha) - \sin(\pi + \alpha)}{\cos(\pi + \alpha)} + \frac{1}{\ctg \alpha}$	$-\sin \alpha \tg \alpha$

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97	$\frac{\cos^2 \alpha - \cos^4(\pi + \alpha)}{1 - \sin^2(\pi + \alpha)} - \sin^2(\pi + \alpha)$	0
98	$\frac{\operatorname{ctg}(\pi + \alpha)}{\operatorname{ctg}^2(\pi + \alpha) + 1} + \cos \alpha (\operatorname{tg}^2(\pi + \alpha) + 1)$	$\sin \alpha \cos \alpha + \sec \alpha$
99	$\sin(\pi + \alpha) \cos(\pi + \alpha) \operatorname{cosec}(\pi + \alpha) - \frac{1 - \sin^2(\pi + \alpha)}{\cos \alpha}$	$-2 \cos \alpha$
100	$\frac{1 - \sin(\pi + \alpha) - \sin^2 \alpha}{\sin(\pi + \alpha) \cos(\pi + \alpha)} + \frac{\cos(\pi + \alpha)}{1 - \sin^2(\pi + \alpha)}$	$\operatorname{ctg} \alpha$
101	$\frac{1 + \sec^2(360^\circ - \alpha) (\sin^2(360^\circ - \alpha) + 1)}{2 \sin \alpha \sec^2(360^\circ - \alpha)}$	$\operatorname{cosec} \alpha$
102	$\frac{\sin(360^\circ - \alpha) \cos(360^\circ - \alpha)}{1 - \sin^2 \alpha} + \frac{1}{\operatorname{ctg}(360^\circ - \alpha)}$	$-2 \operatorname{tg} \alpha$
103	$\frac{\operatorname{tg}^2(360^\circ - \alpha)}{1 - \operatorname{tg}^2(360^\circ - \alpha)} - \operatorname{ctg}(360^\circ - \alpha)$	$\frac{\operatorname{ctg} \alpha + \operatorname{tg}^2 \alpha - \operatorname{tg} \alpha}{1 - \operatorname{tg}^2 \alpha}$
104	$\cos^2(360^\circ - \alpha) + \frac{1}{\operatorname{ctg}^2(360^\circ - \alpha) + 1}$	1
105	$\frac{1}{\operatorname{cosec}^2(360^\circ - \alpha)} + \cos(360^\circ - \alpha) \left(\sin(360^\circ - \alpha) + \frac{1}{\sec \alpha} \right)$	$1 - \sin \alpha \cos \alpha$
106	$\frac{1}{\cos(2\pi - \alpha)(1 + \operatorname{tg}^2(2\pi - \alpha))} + \sec(2\pi - \alpha)$	$(2 + \operatorname{tg}^2 \alpha) \cos \alpha$
107	$-\sin(2\pi - \alpha) \operatorname{tg} \alpha + \frac{1}{\operatorname{cosec}(2\pi - \alpha)}$	$\sin \alpha (\operatorname{tg} \alpha - 1)$
108	$\frac{\sin^2(2\pi - \alpha)}{1 - \sin^2 \alpha} - \frac{1 - \cos^2(2\pi - \alpha)}{\cos^2 \alpha}$	0
109	$\operatorname{cosec}(2\pi - \alpha)(\cos^2 \alpha - 2 \cos^2(2\pi - \alpha) + 1)$	$-\sin \alpha$
110	$\sin(2\pi - \alpha)(\cos^2(2\pi - \alpha) - 1) \frac{1}{\operatorname{tg}^3(2\pi - \alpha)}$	$-\cos^3 \alpha$
111	$(1 - \cos(-45^\circ) + \sin(-30^\circ)) \operatorname{tg}^2(-60^\circ)$	$\frac{3(1 - \sqrt{2})}{2}$
112	$\frac{\sin(-90^\circ) + \sec(-45^\circ)}{\cos(-60^\circ)}$	$2(\sqrt{2} - 1)$

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113	$\cosec(-30^\circ)(\cos^2(-90^\circ) + \cos(-45^\circ)) + 1$	$1 - \sqrt{2}$
114	$2 \sen(-60^\circ) \cos(-30^\circ) + \tg(-45^\circ)$	$-\frac{5}{2}$
115	$\ctg(-45^\circ) + \frac{1}{\cos(-270^\circ) + \cosec(-30^\circ)}$	$-\frac{3}{2}$
116	$\tg\left(-\frac{\pi}{3}\right)\left(\ctg\frac{\pi}{4} + \ctg\left(-\frac{\pi}{6}\right)\right)$	$\sqrt{3}(\sqrt{3} - 1)$
117	$\sec(-\pi) + \tg\frac{\pi}{3} + \frac{1}{\cosec\frac{\pi}{2}}$	$\sqrt{3}$
118	$\left(1 - \sen\left(-\frac{\pi}{2}\right)\right)\left(1 + \cos\frac{\pi}{3}\right) - 1$	2
119	$2\left(\tg\left(-\frac{\pi}{6}\right) - \sen\left(-\frac{\pi}{4}\right)\right)\left(\cos\pi + \ctg\left(-\frac{\pi}{6}\right) + 1\right)$	$2 - \sqrt{6}$
120	$\frac{1 + \cos\left(-\frac{\pi}{3}\right)}{1 - \cos\left(-\frac{\pi}{3}\right)} + \frac{1}{\sec\left(-\frac{\pi}{3}\right)}$	$\frac{7}{2}$

di riepilogo con angoli notevoli, superiori a 360° e angoli associati

121	$\sen^2 15^\circ$	$\frac{2 - \sqrt{3}}{4}$
122	$\cos 75^\circ \cos 15^\circ$	$\frac{1}{4}$
123	$\frac{\tg^2 22,5^\circ}{4} + \sen 45^\circ$	$\frac{3}{4}$
124	$\frac{\cos 72^\circ}{\sen^2 30^\circ} + \tg 45^\circ$	$\sqrt{5}$
125	$\tg 7,5^\circ \tg 67,5^\circ - 3 \tg 30^\circ$	$-\sqrt{2}$
126	$\tg 15^\circ + \frac{\tg 21^\circ + \tg 39^\circ}{1 - \tg 21^\circ \tg 39^\circ}$	2
127	$\sen 18^\circ \tg 9^\circ$	$1 - \frac{\sqrt{10 + 2\sqrt{5}}}{4}$
128	$\frac{\sen 72^\circ \sen 36^\circ}{\sen 18^\circ} + \tg^2 72^\circ$	$\frac{25 + 9\sqrt{5}}{4}$

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129	$(\sin 18^\circ \tan 9^\circ)^2 + 2 \cos 18^\circ$	$\frac{13 + \sqrt{5}}{8}$
130	$(\sin 162^\circ + \sin 126^\circ) \operatorname{cosec} 60^\circ$	$\frac{\sqrt{15}}{3}$
131	$\cos^2 54^\circ \sec^2 36^\circ$	$5 - 2\sqrt{5}$
132	$(2 \sin^2 67,5^\circ - \cos 45^\circ) \cotg 22,5^\circ$	$1 + \sqrt{2}$
133	$\tan 37,5^\circ + \sqrt{2} \tan 67,5^\circ$	$\sqrt{3}(1 + \sqrt{2})$
134	$\cos 85^\circ \cos 13^\circ + \sin 85^\circ \sin 13^\circ$	$\frac{\sqrt{5} - 1}{4}$
135	$\frac{1}{2}(\sqrt{3} \cos 6^\circ - \sin 6^\circ)$	$\frac{\sqrt{5} + 1}{4}$
136	$(\sqrt{3} - \tan 24^\circ)/(1 + \sqrt{3} \tan 24^\circ)$	$\sqrt{5 - 2\sqrt{5}}$
137	$(\tan 22^\circ - \tan 5^\circ) \cotg 17^\circ \cotg 5^\circ / (\cotg 5^\circ + \tan 22^\circ)$	1
138	$16 \sin^5 18^\circ - 20 \sin^3 18^\circ + 5 \sin 18^\circ$ [esercizio difficile]	1
139	$\cos 9^\circ - \sin 9^\circ$ [esercizio difficile]	$\frac{\sqrt{5-\sqrt{5}}}{2}$
140	$8 \cos^3 20^\circ - 6 \cos 20^\circ$ [esercizio difficile]	1
141	$\sin^2(180^\circ - \alpha) - 1 + \cos(360^\circ - \alpha) + \cos^2(-\alpha)$	$\cos \alpha$
142	$2 \sin^2(180^\circ + \alpha) + \cos^4(180^\circ - \alpha) \tan^2(180^\circ + \alpha) - \sin^4(180^\circ - \alpha)$	$\sin^2 \alpha (3 - 2 \sin^2 \alpha)$
143	$\frac{a \cos(-45^\circ) - \tan(-30^\circ)}{-\frac{3}{2} b \operatorname{cosec}(-30^\circ)}$	$\frac{3a\sqrt{2} + 2\sqrt{3}}{18b}$
144	$\sec(360^\circ - \alpha)(\sin(360^\circ - \alpha) \cos(360^\circ - \alpha) - 1) + \frac{\tan \alpha}{\sin(180^\circ - \alpha)}$	$-\sin \alpha$
145	$\frac{1 - \cos^2(360^\circ - \alpha)}{\sin(180^\circ + \alpha) \cos(360^\circ - \alpha)} + \frac{1}{\sin \alpha \cos(180^\circ + \alpha)}$	$-\frac{\sin^2 \alpha + 1}{\sin \alpha \cos \alpha}$

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146	$\left(\frac{ctg^2(-30^\circ)}{a \sen(-30^\circ)} \frac{b^2 \cos(-30^\circ)}{tg(-30^\circ)} \right)^{\frac{1}{2}}$	$\frac{3\sqrt{ab^2}}{a}$
147	$cosec(360^\circ - \alpha) - \cos(180^\circ + \alpha) ctg(180^\circ - \alpha)$	$\frac{\sen^2 \alpha - 2}{\sen \alpha}$
148	$\cos^2(\pi - \alpha) tg \alpha - \cos^2(-\alpha) ctg(\pi - \alpha)$	$ctg \alpha$
149	$\frac{\sqrt{a}}{2} ctg^2(-45^\circ) + \frac{\sqrt{b}}{a} \frac{\sen(-45^\circ)}{1 + \cos(-60^\circ)}$	$\frac{\sqrt{a}}{2} - \frac{\sqrt{2b}}{3a}$
150	$a \cos^2(-30^\circ) (4b^2 \cos(-45^\circ) + 1)$	$\frac{3}{4}a(1 + 2\sqrt{2}b^2)$
151	$\cos \alpha - \frac{\cos^2(\pi + \alpha) - \sen^2(2\pi - \alpha)}{\sen(2\pi - \alpha) - \cos(2\pi - \alpha)}$	$2 \cos \alpha - \sen \alpha$
152	$\frac{3b \left(tg\left(-\frac{\pi}{3}\right) - ctg\left(-\frac{\pi}{3}\right) \right)}{2a \left(tg\left(-\frac{\pi}{6}\right) + ctg\left(\frac{\pi}{6}\right) \right)}$	$-\frac{3b}{2a}$
153	$\sen(\pi + \alpha) cosec(2\pi - \alpha)(tg(-\alpha) + ctg \alpha)$	$\frac{1 - 2 \sen^2 \alpha}{\sen \alpha \cos \alpha}$
154	$\frac{(b+c) \sec(-45^\circ) + (b-c) \cosec(-45^\circ)}{tg(-60^\circ) ctg(-30^\circ)}$	$\frac{2\sqrt{2}c}{3}$
155	$\cos(2\pi + \alpha) tg(\pi - \alpha) + \sen(\pi - \alpha) ctg(2\pi + \alpha)$	$\cos \alpha - \sen \alpha$
156	$b^3 \cos\left(-\frac{\pi}{4}\right) \left(1 + tg^2\left(\frac{\pi}{4}\right)\right) + \sqrt[3]{b} ctg^2\left(-\frac{\pi}{3}\right)$	$\sqrt{2}b^3 + \frac{1}{3}\sqrt[3]{b}$
157	$\frac{2a + \sen\left(-\frac{\pi}{3}\right)}{\cos^2\left(-\frac{\pi}{3}\right)} + \frac{3b - \cos\left(-\frac{\pi}{6}\right)}{\sen^2\left(-\frac{\pi}{6}\right)}$	$4(2a - \sqrt{3} + 3b)$
158	$cosec(\pi - \alpha)(1 - \sen^2(\pi + \alpha))$	$ctg \alpha \cos \alpha$
159	$\frac{3}{2}\sqrt{a} tg^2\left(-\frac{\pi}{4}\right) \frac{\sec\left(-\frac{\pi}{4}\right)}{\cosec\left(-\frac{\pi}{4}\right)} \frac{\sqrt{a}}{a}$	$-\frac{3}{2}$
160	$\left(2a \sen\left(-\frac{\pi}{3}\right) - 2b \cos\left(-\frac{\pi}{3}\right)\right)^2 + \frac{\sqrt{b}}{b}$	$(\sqrt{3}a + b)^2 + \frac{\sqrt{b}}{b}$

risolubili con le formule di addizione e sottrazione

161	$\sen(\alpha + \beta) \sen(\alpha - \beta)$	$\sen^2 \alpha - \sen^2 \beta$
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Espressioni goniometriche

162	$\cos(\alpha + \beta) \cos(\alpha - \beta)$	$\cos^2 \alpha - \sin^2 \beta$
163	$\cos(\alpha - \beta) \cos \alpha + \sin(\alpha - \beta) \sin \alpha$	$\cos \beta$
164	$\frac{\cos(\alpha + \beta) + \cos(\alpha - \beta)}{\sin(\alpha + \beta) + \sin(\alpha - \beta)}$	$\operatorname{ctg} \alpha$
165	$\frac{\cos(\alpha - \beta)}{\sin \beta \cos \alpha}$	$\operatorname{tg} \alpha + \operatorname{ctg} \beta$
166	$\frac{\sin(\alpha + \beta)}{\sin(\alpha - \beta)}$	$\frac{\operatorname{tg} \alpha + \operatorname{tg} \beta}{\operatorname{tg} \alpha - \operatorname{tg} \beta}$
167	$\operatorname{tg}(\alpha + \beta) \operatorname{tg}(\alpha - \beta)$	$\frac{\operatorname{tg}^2 \alpha - \operatorname{tg}^2 \beta}{1 - \operatorname{tg}^2 \alpha \operatorname{tg}^2 \beta}$
168	$\operatorname{tg}(\alpha + \beta) \frac{\operatorname{ctg} \beta}{\operatorname{ctg} \alpha}$	$\frac{\operatorname{tg}^2 \alpha + \operatorname{tg} \alpha \operatorname{tg} \beta}{\operatorname{tg} \beta - \operatorname{tg} \alpha \operatorname{tg}^2 \beta}$
169	$\frac{\operatorname{tg}(\alpha + \beta)}{\operatorname{ctg}(\alpha - \beta)}$	$\frac{\operatorname{tg} \alpha \operatorname{ctg} \beta - \operatorname{tg} \beta \operatorname{ctg} \alpha}{\operatorname{ctg} \alpha \operatorname{ctg} \beta - \operatorname{tg} \alpha \operatorname{tg} \beta}$
170	$\frac{\operatorname{tg}(\alpha - \beta) + \operatorname{tg} \beta}{\operatorname{tg}(\alpha + \beta) - \operatorname{tg} \beta}$	$\frac{\cos(\alpha + \beta)}{\cos(\alpha - \beta)}$

risolubili con le formule di duplicazione e bisezione

171	$\sin^2 2\alpha + \cos 2\alpha + 4 \sin^4 \alpha$	$2 \sin^2 \alpha + 1$
172	$(1 + \cos 2\alpha) \operatorname{tg} \alpha$	$\sin 2\alpha$
173	$\frac{2 - \sin^2 2\alpha}{2}$	$\sin^4 \alpha + \cos^4 \alpha$
174	$\sin 2\alpha (\operatorname{tg} \alpha + \operatorname{ctg} \alpha)$	2
175	$\frac{1 - \cos 2\alpha}{2} (\operatorname{ctg}^2 \alpha - 1)$	$\cos 2\alpha$
176	$\frac{1}{2} \operatorname{tg} 2\alpha (1 + \operatorname{tg} \alpha)$	$\frac{\operatorname{tg} \alpha}{1 - \operatorname{tg} \alpha}$
177	$\frac{\operatorname{tg} 2\alpha}{4 \sin \alpha \operatorname{ctg} 2\alpha}$	$\frac{\sin^2 \alpha \cos^2 \alpha}{\cos^2(2\alpha)}$

Espressioni goniometriche

178	$2 \operatorname{tg}^2 \alpha \operatorname{sen}^2 \frac{\alpha}{2} + \operatorname{tg} \alpha \operatorname{sen} \alpha$	$\operatorname{tg}^2 \alpha$
179	$\frac{1 - \cos \alpha}{2} \left(\operatorname{ctg}^2 \frac{\alpha}{2} - 1 \right)$	$\cos \alpha$
180	$\frac{1}{1 - \operatorname{tg}^2 \frac{\alpha}{2}} - \frac{1}{1 - \operatorname{ctg}^2 \frac{\alpha}{2}}$	$\frac{1}{\cos \alpha}$

risolubili con le formule di prostaferesi e Werner

181	$\cos(60^\circ + \alpha) + \cos(60^\circ - \alpha)$	$\cos \alpha$
182	$\operatorname{ctg}(45^\circ + \alpha) + \operatorname{ctg}(45^\circ - \alpha)$	$\frac{2}{\cos 2\alpha}$
183	$\operatorname{tg} 7\alpha + \operatorname{tg} 3\alpha$	$\frac{\operatorname{sen} 10\alpha}{\cos 7\alpha \cos 3\alpha}$
184	$\operatorname{sen} \alpha \operatorname{sen} \beta - \frac{1}{2} \cos(\alpha - \beta)$	$-\frac{1}{2} \cos(\alpha + \beta)$
185	$\frac{\operatorname{sen} \alpha - \operatorname{sen} \beta}{\cos \alpha + \cos \beta}$	$\operatorname{tg} \frac{\alpha - \beta}{2}$
186	$\operatorname{sen} \left(\frac{\pi}{3} + \alpha \right) + \operatorname{sen} \left(\frac{\pi}{3} - \alpha \right)$	$\sqrt{3} \cos \alpha$
187	$\operatorname{tg} \left(\frac{\pi}{4} + \alpha \right) - \operatorname{tg} \left(\frac{\pi}{4} - \alpha \right)$	$2 \operatorname{tg} 2\alpha$
188	$\frac{\operatorname{sen} \left(\frac{\pi}{3} + \alpha \right) + \cos \left(\frac{5}{6}\pi - \alpha \right)}{\cos \left(\frac{\pi}{3} + \alpha \right) + \operatorname{sen} \left(\frac{5}{6}\pi - \alpha \right)}$	$\operatorname{tg} \alpha$
189	$2 \operatorname{sen} \alpha \operatorname{cos} 3\alpha$	$\operatorname{sen} 4\alpha - \operatorname{sen} 2\alpha$
190	$\frac{\operatorname{cos} \left(\alpha - \frac{\pi}{4} \right) \operatorname{sen} \left(\frac{3}{4}\pi + \alpha \right)}{\operatorname{cos} \alpha + \operatorname{sen} \alpha}$	$\frac{1}{2} (\operatorname{cos} \alpha - \operatorname{sen} \alpha)$

di riepilogo con formule goniometriche

191	$\frac{1}{2} \operatorname{sen} 2(\alpha + \beta)$	$\operatorname{sen} \alpha \operatorname{cos} \alpha \operatorname{cos} 2\beta + \operatorname{sen} \beta \operatorname{cos} \beta \operatorname{cos} 2\alpha$
192	$\operatorname{cos}^4 \alpha - \operatorname{sen}^4 \alpha$	$\operatorname{cos} 2\alpha$

Espressioni goniometriche

193	$\cos^4 \frac{\alpha}{2} - \sin^4 \frac{\alpha}{2}$	$\cos \alpha$
194	$\frac{\cos 8\alpha + \cos \alpha}{\cos 8\alpha - \cos \alpha}$	$-\operatorname{ctg} \frac{9}{2}\alpha \operatorname{ctg} \frac{7}{2}\alpha$
195	$\frac{\sin(3\alpha + \beta) \sin(3\alpha - \beta) - \sin(\alpha + \beta) \sin(\alpha - \beta)}{\sin 4\alpha \sin 2\alpha}$	1
196	$2 \operatorname{tg} \alpha \sin^2 \frac{\alpha}{2} + \sin \alpha$	$\operatorname{tg} \alpha$
197	$\sin \alpha \cos(\alpha + \beta) - \cos \alpha \sin(\alpha + \beta)$	$\cos\left(\frac{\pi}{2} + \beta\right)$
198	$\frac{\sin^2 \alpha - \sin^2 \beta}{\cos^2 \alpha - \cos^2 \beta}$	-1
199	$\frac{1 + \operatorname{ctg} \frac{\alpha}{2} \operatorname{tg} \frac{\alpha + \beta}{2}}{\operatorname{ctg} \frac{\alpha}{2} - \operatorname{tg} \frac{\alpha + \beta}{2}}$	$\operatorname{tg}\left(\alpha + \frac{\beta}{2}\right)$
200	$\frac{2 \sin 3\alpha \sin 8\alpha}{\sin 5\alpha + \sin 8\alpha}$	$\frac{\cos 5\alpha - \cos 11\alpha}{2 \sin \frac{13}{2}\alpha \cos \frac{3}{2}\alpha}$
201	$\frac{2 \operatorname{tg}\left(\frac{\pi}{2} - \alpha\right)}{1 + [\operatorname{ctg}(\pi - \alpha)]^2} - [\cos\left(\frac{\pi}{2} - \alpha\right) + \sin\left(\frac{\pi}{2} - \alpha\right)]$	$\sin 2\alpha - \sin \alpha - \cos \alpha$

con funzioni goniometriche inverse

202	$\operatorname{tg}(\arccos\left(-\frac{\sqrt{2}}{2}\right))$	-1
203	$\operatorname{tg}(\arcsen\left(\frac{\sqrt{3}}{2}\right))$	$\sqrt{3}$
204	$\frac{3}{4} + \operatorname{cotg}\left(\arcsen\left(\frac{\sqrt{2}}{2}\right)\right) - \frac{1}{2} \cos(\operatorname{arccotg}(0))$	$\frac{7}{4}$
205	$\sqrt{2} \sin\left(\arccos\left(\frac{\sqrt{2}}{2}\right)\right) - \frac{1}{2} + \frac{3}{2} \operatorname{tg}(\operatorname{arccotg}(\sqrt{3}))$	$\frac{1 + \sqrt{3}}{2}$
206	$\sin(\operatorname{arctg}(1))$	$\frac{\sqrt{2}}{2}$
207	$\operatorname{cosec}(\operatorname{arctg}\left(-\frac{\sqrt{3}}{3}\right))$	-2
208	$\cos(\operatorname{arccotg}(-\sqrt{3}))$	$\frac{\sqrt{3}}{2}$

Espressioni goniometriche

209	$\sin(\arccos(1))$	0
210	$\sin(\operatorname{arctg}\sqrt{3})$	$\frac{\sqrt{3}}{2}$