

Disequazioni goniometriche

elementari

1	$\operatorname{sen} x > \frac{1}{2}$	$\frac{\pi}{6} + 2k\pi < x < \frac{5}{6}\pi + 2k\pi$
2	$\operatorname{tg} x > \sqrt{3}$	$\frac{\pi}{3} + k\pi < x < \frac{\pi}{2} + k\pi$
3	$\operatorname{cos} x > -\frac{1}{2}$	$-\frac{2}{3}\pi + 2k\pi < x < \frac{2}{3}\pi + 2k\pi$
4	$\operatorname{cot} g x < -1$	$\frac{3}{4}\pi + k\pi < x < (k+1)\pi$
5	$2\operatorname{sen} x + \sqrt{2} > 0$	$-\frac{\pi}{4} + 2k\pi < x < \frac{5}{4}\pi + 2k\pi$
6	$2\operatorname{cos} x + \sqrt{2} > 0$	$-\frac{3}{4}\pi + 2k\pi < x < \frac{3}{4}\pi + 2k\pi$
7	$\operatorname{tg} x < -\sqrt{3}$	$\frac{\pi}{2} + k\pi < x < \frac{2}{3}\pi + k\pi$
8	$\operatorname{tg} x < 2 + \sqrt{3}$	$-\frac{\pi}{2} + k\pi < x < \frac{5}{12}\pi + k\pi$
9	$3\operatorname{sen} x - 10 > 0$	<i>impossibile</i>
10	$2\operatorname{cos} x + \sqrt{3} \geq 0$	$-\frac{5}{6}\pi + 2k\pi \leq x \leq \frac{5}{6}\pi + 2k\pi$
11	$\operatorname{cot} g x < -\frac{\sqrt{3}}{3}$	$\frac{2}{3}\pi + k\pi < x < (k+1)\pi$

di secondo grado

12	$2\operatorname{sen}^2 x + 5\operatorname{cos} x - 4 > 0$	$-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{3} + 2k\pi$
13	$2\operatorname{sen}^2 x - \sqrt{2}\operatorname{sen} x > 0$	$\frac{\pi}{4} + 2k\pi < x < \frac{3}{4}\pi + 2k\pi \cup (2k+1)\pi < x < 2(k+1)\pi$
14	$3\operatorname{tg}^2 x - 1 > 0$	$\frac{\pi}{6} + k\pi < x < \frac{\pi}{2} + k\pi \cup \frac{\pi}{2} + k\pi < x < \frac{5}{6}\pi + k\pi$
15	$2\operatorname{cos}^2 x - \sqrt{2}\operatorname{cos} x > 0$	$\frac{\pi}{2} + 2k\pi < x < \frac{3}{2}\pi + 2k\pi \cup -\frac{\pi}{4} + 2k\pi < x < \frac{\pi}{4} + 2k\pi$
16	$8\operatorname{cos}^2 x + 2\operatorname{cos} x - 3 < 0$	$-\arccos\left(-\frac{3}{4}\right) + 2k\pi < x < -\frac{\pi}{3} + 2k\pi \cup$ $\frac{\pi}{3} + 2k\pi < x < \arccos\left(-\frac{3}{4}\right) + 2k\pi$
17	$\operatorname{tg}^2 x + 2\operatorname{tg} x + 3 < 0$	<i>impossibile</i>
18	$2\operatorname{cos}^2 x - \operatorname{sen} x - 1 < 0$	$\frac{\pi}{6} + 2k\pi < x < \frac{5}{6}\pi + 2k\pi$
19	$3\operatorname{cot} g^2 x - 4\sqrt{3}\operatorname{cot} g x + 3 > 0$	$\frac{\pi}{3} + k\pi < x < (k+1)\pi \cup (k+1)\pi < x < \frac{7}{6}\pi + k\pi$
20	$\operatorname{tg}^2 x + (\sqrt{3} + 1)\operatorname{tg} x + \sqrt{3} > 0$	$x \neq k\pi \cup x \neq \pm \frac{\pi}{2}$
21	$2\operatorname{cos}^2 x + \sqrt{3}\operatorname{sen} x - 2 > 0$	$2k\pi < x < \frac{\pi}{3} + 2k\pi \cup \frac{2}{3}\pi + 2k\pi < x < (2k+1)\pi$

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22	$\cos 2x + \operatorname{sen} x \geq 0$	$-\frac{\pi}{6} + 2k\pi \leq x \leq \frac{7}{6}\pi + 2k\pi$
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23	$\sqrt{3}\operatorname{sen} x + 3\cos x > 0$	$-\frac{\pi}{3} + 2k\pi < x < \frac{2}{3}\pi + 2k\pi$
24	$\sqrt{3}\operatorname{sen} x + 3\cos x - \sqrt{3} > 0$	$-\frac{\pi}{6} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
25	$\sqrt{3}\operatorname{sen} x - \cos x - 1 < 0$	$-\pi + 2k\pi < x < \frac{\pi}{3} + 2k\pi$
26	$\cos x + \sqrt{3}\operatorname{sen} x - \sqrt{3} > 0$	$\frac{\pi}{6} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
27	$\cos x - \operatorname{sen} x + 1 > 0$	$-\pi + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
28	$\cos x + \operatorname{sen} x - \sqrt{2} \geq 0$	$x = \frac{\pi}{4} + 2k\pi$
29	$\cos x + \sqrt{3}\operatorname{sen} x - \sqrt{3} \geq 0$	$\frac{\pi}{6} + 2k\pi \leq x \leq \frac{\pi}{2} + 2k\pi$
30	$\operatorname{sen}\left(x - \frac{\pi}{3}\right) + \cos\left(\frac{4}{3}\pi - x\right) - 1 < 0$	$-\frac{2}{3}\pi + 2k\pi < x < \frac{5}{6}\pi + 2k\pi$
31	$\operatorname{sen} 2x - \cos x + 1 > 2\operatorname{sen} x$	$2k\pi < x < \frac{\pi}{6} + 2k\pi \cup \frac{5}{6}\pi + 2k\pi < x < 2k\pi$
32	$2\cos x - 2\operatorname{sen}\left(-x - \frac{2}{3}\pi\right) - 1 < 0$	$-\pi + 2k\pi < x < \frac{\pi}{2} + 2k\pi \cup \frac{\pi}{3} + 2k\pi < x < \pi + 2k\pi$
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33	$\operatorname{sen}^2 x - 3\cos^2 x \leq 0$	$-\frac{\pi}{3} + 2k\pi \leq x \leq \frac{\pi}{3} + 2k\pi$
34	$\cos^2 x + (\sqrt{3} - 1)\operatorname{sen} x \cos x - \sqrt{3}\operatorname{sen}^2 x > 0$	$-\frac{\pi}{6} + k\pi < x < \frac{\pi}{4} + k\pi$
35	$3\operatorname{sen}^2 x - 2\operatorname{sen} x \cos x - \cos^2 x < 0$	$-\arctg \frac{1}{3} + k\pi < x < \frac{\pi}{4} + k\pi$
36	$\operatorname{sen}^2 x - (\sqrt{3} + 1)\operatorname{sen} x \cos x + \sqrt{3}\cos^2 x > 0$	$-\frac{2}{3}\pi + k\pi < x < \frac{\pi}{4} + k\pi$
37	$\operatorname{sen}^2 x + 4\operatorname{sen} x \cos x + 3\cos^2 x > 0$	$-\frac{\pi}{4} + k\pi < x < \pi - \arctg 3 + k\pi$
38	$2\sqrt{3}\cos^2 x - 2\operatorname{sen} x \cos x - \sqrt{3} \leq 0$	$\frac{\pi}{6} + k\pi < x < \frac{2}{3}\pi + k\pi$
39	$3\cos^2 x + 2\operatorname{sen} 2x + 2\operatorname{sen}^2 x > 2$	$-\arctg \frac{1}{4} + k\pi < x < \frac{\pi}{2} + k\pi$
40	$\operatorname{sen}^2 x + 4\operatorname{sen} x \cos x + \cos^2 x < 0$	$\frac{\pi}{12} + k\pi < x < \frac{5}{12}\pi + k\pi$
41	$5\operatorname{sen}^2 x - \sqrt{3}\operatorname{sen} 2x - \cos^2 x < 2$	$-\frac{\pi}{6} + k\pi < x < \frac{\pi}{3} + k\pi$
42	$3\operatorname{sen}^2 x + \sqrt{3}\operatorname{sen} 2x + \cos^2 x > 0$	$\forall x \in \mathfrak{R} - \left\{\frac{5}{6}\pi + k\pi\right\}$

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43	$(3 + \sqrt{3})\text{sen}^2 x + (\sqrt{3} - 1)\text{sen}x\text{cos}x + 2\text{cos}^2 x > 3$	$\frac{\pi}{6} + k\pi < x < \frac{3}{4}\pi + k\pi$
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44	$3 \text{tg} x > \sqrt{3}$	$\frac{\pi}{6} + k\pi < x < \frac{\pi}{2} + k\pi$
45	$2 \text{sen} x - \sqrt{3} \geq 0$	$\frac{\pi}{3} + 2k\pi \leq x \leq \frac{2}{3}\pi + 2k\pi$
46	$\text{cos} x - 2 \geq 0$	<i>impossibile</i>
47	$2 \text{sen} x + \sqrt{3} > 0$	$-\frac{\pi}{3} + 2k\pi < x < \frac{4}{3}\pi + 2k\pi$
48	$2 \text{sen}^2 x - (2 - \sqrt{3}) \text{sen} x - \sqrt{3} \leq 0$	$-\frac{\pi}{3} + 2k\pi \leq x \leq \frac{4}{3}\pi + 2k\pi$
49	$\text{cos}^2 x + \text{cos} x \geq 0$	$-\frac{\pi}{2} + 2k\pi \leq x \leq \frac{\pi}{2} + 2k\pi \cup$ $x = \pi + 2k\pi$
50	$\text{cos}^2 x + 1 \leq 0$	<i>impossibile</i>
51	$2 \text{cos}^2 x + 3 \text{cos} x + 1 > 0$	$-\frac{2}{3}\pi + 2k\pi < x < \frac{2}{3}\pi + 2k\pi$
52	$2 \text{sen}^2 x - \text{sen} x - 1 > 0$	$-\frac{5}{6}\pi + 2k\pi < x < -\frac{\pi}{6} + 2k\pi$
53	$2 \text{sen}^2 x - 3 \text{sen} x + 1 < 0$	$\frac{\pi}{6} + 2k\pi < x < \frac{5}{6}\pi + 2k\pi, x \neq \frac{\pi}{2}$
54	$2 \text{cos}^2 x - 3 \text{cos} x + 1 < 0$	$-\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{3} + 2k\pi, x \neq 0$
55	$\text{cos} 2x + \text{cos} x < 0$	$\frac{\pi}{3} + 2k\pi < x < \frac{5}{3}\pi + 2k\pi, x \neq \pi$
56	$\text{sen} x \text{cos} x > 0$	$k\pi < x < \frac{\pi}{2} + k\pi$
57	$4 \text{sen}^2 x - 2\sqrt{3} \text{sen} x \text{cos} x - 2 \text{cos}^2 x - 1 > 0$	$\frac{\pi}{3} + k\pi < x < \frac{5}{6}\pi + k\pi \cup x \neq \frac{\pi}{2} + k\pi$
58	$\text{sen}^2 x + \text{sen} x \text{cos} x < 0$	$-\frac{\pi}{4} + k\pi < x < k\pi$
59	$\sqrt{3} \text{sen} x - \text{cos} x \leq 0$	$-\frac{5}{6}\pi + 2k\pi \leq x \leq \frac{\pi}{6} + 2k\pi$
60	$\sqrt{3} \text{cos} x - \text{sen} x + 1 \geq 0$	$-\frac{5}{6}\pi + 2k\pi \leq x \leq \frac{\pi}{2} + 2k\pi$
61	$\text{sen}^4 x - \text{cos}^4 x < 0$	$-\frac{\pi}{4} + k\pi < x < \frac{\pi}{4} + k\pi$
62	$2 \text{sen}^2 x + 4 \text{cos}^2 x > 5 \text{cos} x$	$\frac{\pi}{3} + 2k\pi < x < \frac{5}{3}\pi + 2k\pi$
63	$\text{cos}^2 x + 2 \text{cos} x < 0$	$\frac{\pi}{2} + 2k\pi < x < \frac{3}{2}\pi + 2k\pi$